



Introduction

Coordinate systems

Kinematic Equations

Robot Description

Inverse Kinematics for Manipulators

Differential motion with homogeneous transformations

Jacobian

Trajectory planning

Trajectory generation

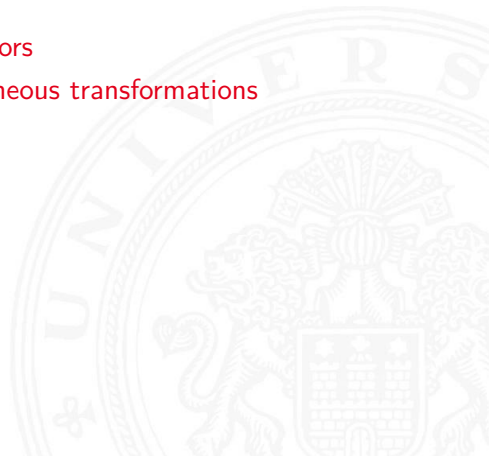
Dynamics

Principles of Walking

- Introduction

- ZMP

- Inverted Pendulum





Stabilizing Full Body Motion

Robot Control

Task-Level Programming and Trajectory Generation

Task-level Programming and Path Planning

Task-level Programming and Path Planning

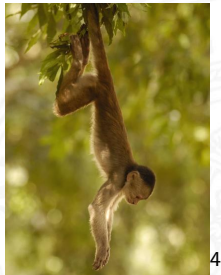
Architectures of Sensor-based Intelligent Systems

Summary

Conclusion and Outlook



- ▶ Enabling locomotion in difficult terrain
- ▶ Legs can be used for other things
- ▶ Necessary to integrate robots in a human environment



³ http://1.bp.blogspot.com/-MhFvPPR5V4/UmifTu4r_OI/AAAAAAAAAFtI/FvJqeWu9Ahc/s1600/13-pictures-of-crazy-goats-on-cliff-transparent.png

⁴ <https://www.allposters.com>

- ▶ Stability
- ▶ Energy consumption
- ▶ Hardware costs
- ▶ Complex control



⁵<https://www.wikihow.com/Recognize-the-Signs-of-Intoxication>

- ▶ Static - Dynamic
- ▶ Passiv - Active
- ▶ 2,4,6,8,... legged
- ▶ Open loop - closed loop
- ▶ This lecture: active bipedal walking, no running

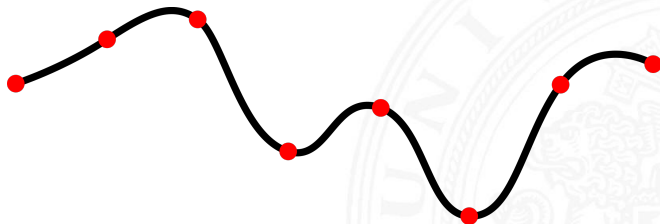


⁶ <https://3c1703fe8d.site.internapcdn.net/newman/gfx/news/hires/2017/1-sixleggedrob-transparent.png>

⁷ <https://asl.ethz.ch/research/legged-robots.html>

Types of Implementing Walking

- ▶ Control Theory
- ▶ Neural Networks
- ▶ Central Pattern Generators
- ▶ Evolutional Computing
- ▶ Expert Solution



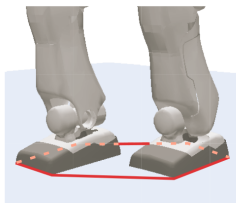
⁸<https://de.wikipedia.org/wiki/Spline-Interpolation>



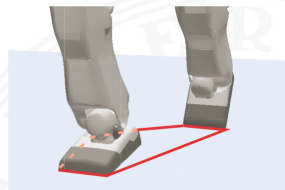
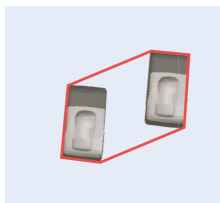
- ▶ Support leg/foot
- ▶ Flying leg/foot
- ▶ Torso / trunk
- ▶ Step / double step
- ▶ Sagittal / lateral



- Convex hull of all ground contact points



(a) Full contact of both feet

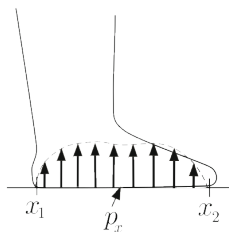


(b) Partial contact

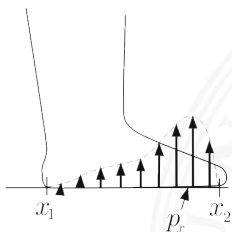
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Center of Pressure (CoP)

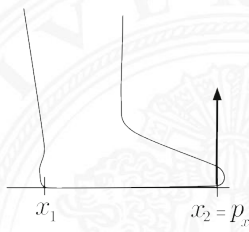
- ▶ Center of ground reaction forces
- ▶ Those can also be horizontal
- ▶ Moment becomes zero
- ▶ Equals the zero moment point (ZMP)



(a) Almost flat



(b) Biased distribution

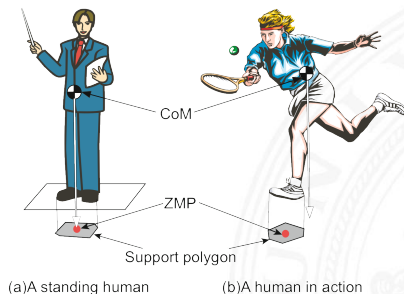


(c) Concentrate at tiptoe 10

¹⁰ Introduction to Humanoid Robotics, Shuji Kajita, 2015

Zero Moment Point (ZMP)

- ▶ When standing, projection of CoM coincides with ZMP
- ▶ When dynamic, CoM outside of support polygon
- ▶ ZMP is always inside support polygon

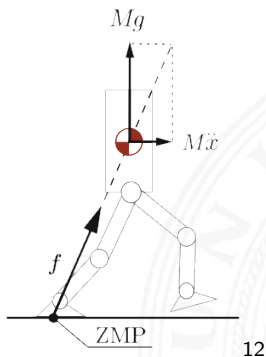


(a) A standing human

(b) A human in action

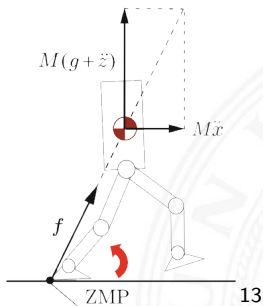
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- ▶ Forces of the robot define position of ZMP
- ▶ Can it get outside of the support polygon?



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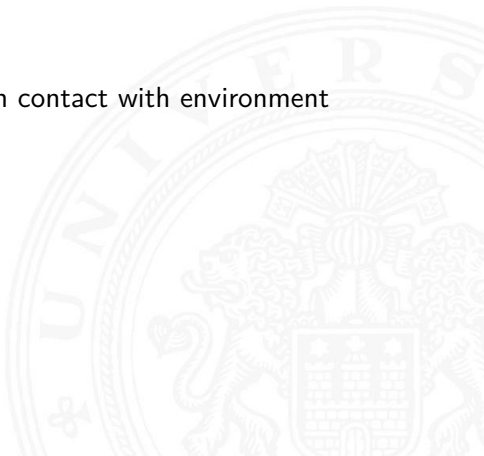
- ▶ No! The ZMP is always in the support polygon
- ▶ If it is on an edge, the robot rotates



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- ▶ Sole slips on ground
- ▶ Other parts of the robot are in contact with environment
- ▶ Ground is not perfectly level

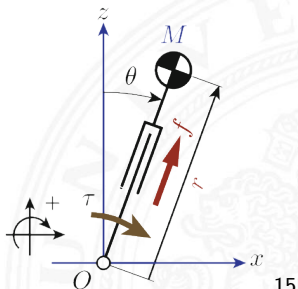
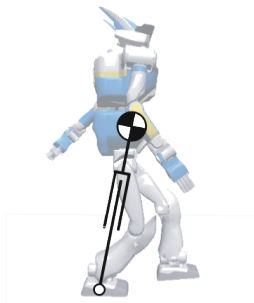




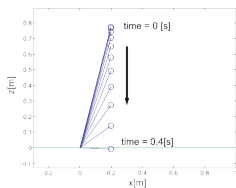
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14 https://www.reddit.com/r/rickandmorty/comments/70t45i/anyone_else_wish_heshe_could_experience_true_level/

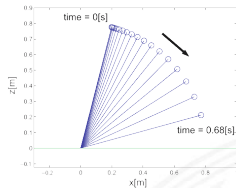
- ▶ Simplest model for walking robot or human
- ▶ Point mass at end of massless telescopic leg
- ▶ f : kick force, τ : torque



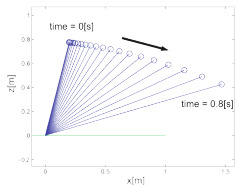
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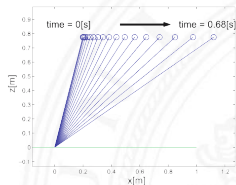
(a) $f = 0$: Free fall of CoM



(b) $f = Mg \cos \theta - Mr \dot{\theta}^2$: Fall down with constant leg length



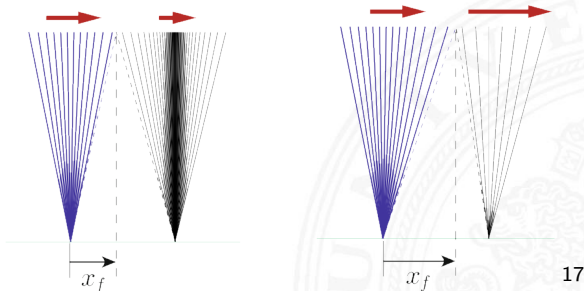
(c) $f = Mg$: Fall down and acceleration



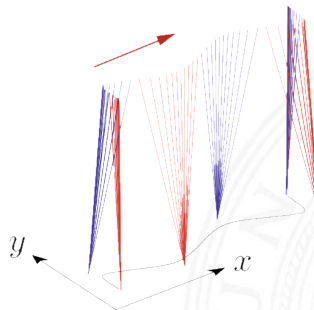
(d) $f = Mg / \cos \theta$: CoM accelerates while keeping the initial height

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- ▶ Considering fixed step length
- ▶ Earlier touchdown of the next step results slow down
- ▶ Later touchdown of the next step results speed ups

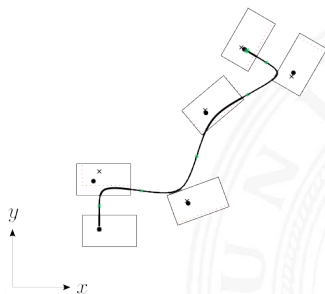


- ▶ Transfer to 3D
- ▶ Introduction of lateral movement



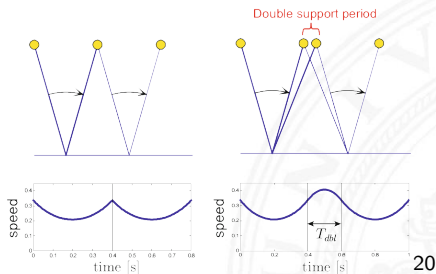
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- ▶ Forward (x)
- ▶ Sideward (y)
- ▶ Turn (yaw)

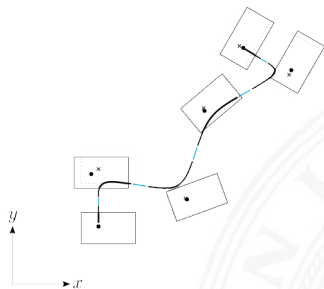


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- ▶ Accelerations are extreme on support change
- ▶ Not feasible in reality
- ▶ Introduction of a double support phase



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Zero Support



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²²<https://thumbs.dreamstime.com/z/running-robot-27653003-transparent.png>



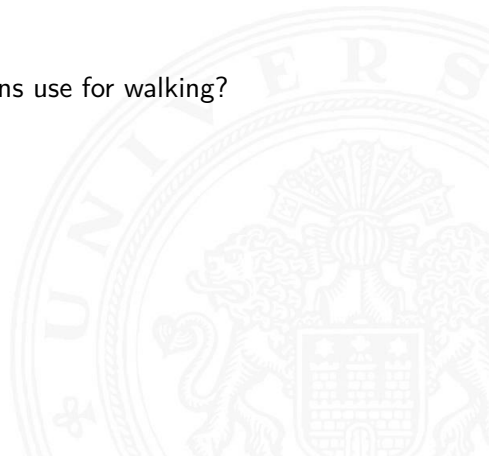
- ▶ Why are we not finished yet?



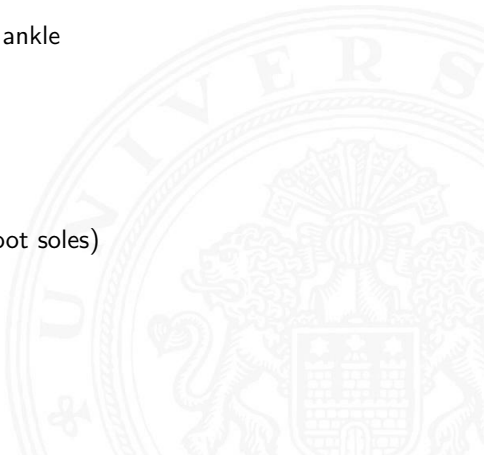


Detecting Instability

Which senses do you think humans use for walking?

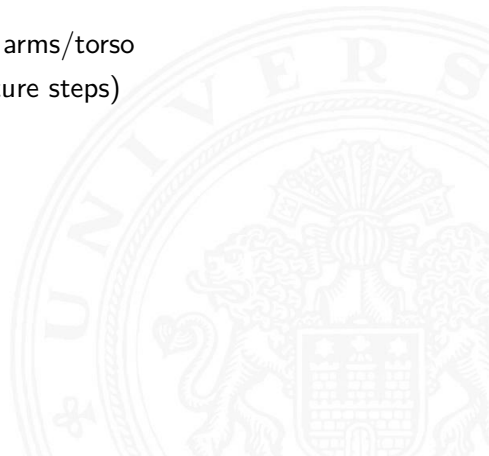


- ▶ Sensors
 - ▶ IMU(s)
 - ▶ Force sensors on foot sole
 - ▶ 6 axis force/torque sensor in ankle
 - ▶ Joint Torques
 - ▶ Camera
- ▶ Model
 - ▶ Joint positions
 - ▶ Link masses and inertia
 - ▶ Rigidity of links (especially foot soles)



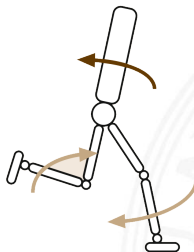


- ▶ Simple stopping
- ▶ Counter movements with the arms/torso
- ▶ Change of step position (capture steps)



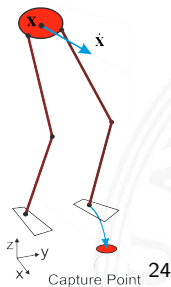
Counter Movements with Upper Body

- ▶ Rotation around edge of support polygon
- ▶ Introduce counter force with arms/torso or flying leg
- ▶ Flying leg is mostly not usable



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- ▶ Capture point is where the robot comes to a complete stop
- ▶ Multiple capture steps may be necessary
- ▶ You can completely base your walking on this



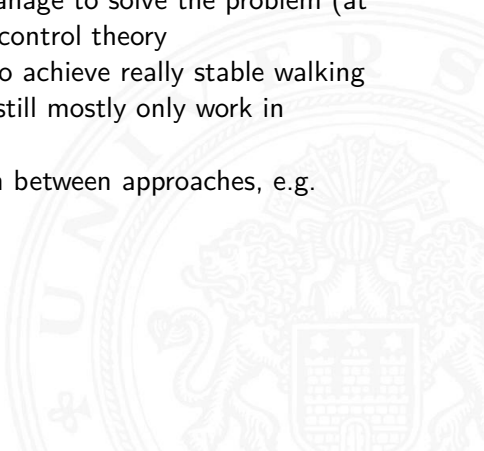
²⁴ <https://ieeexplore.ieee.org/stamp/stamp.jsp?tp=&arnumber=6094435>



- ▶ We will not cover machine learning
- ▶ If you are interested join my lecture in "Intelligent Robotics" in the winter term
- ▶ General approaches are:
 - ▶ Learning parameter of a walking pattern generator (e.g. double support length)
 - ▶ Learning neural networks from scratch
 - ▶ Learning from demonstration
 - ▶ Artificial central pattern generators



- ▶ Some very expensive robot manage to solve the problem (at least most of the time) using control theory
- ▶ Cheaper robots still struggle to achieve really stable walking
- ▶ Machine learning approaches still mostly only work in simulation (reality gap)
- ▶ Working on better comparison between approaches, e.g. EuroBench





BALANCE



System Abilities*

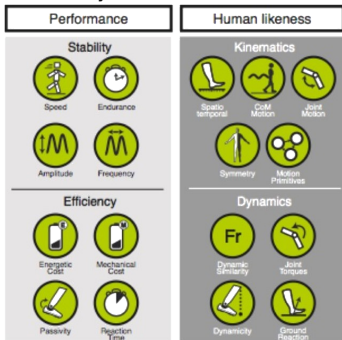
HUMANOIDS



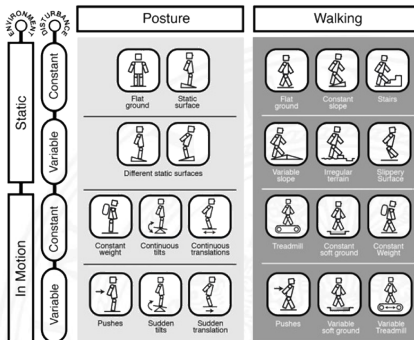
WEARABLE ROBOTS



CLINICAL ASSESSMENT



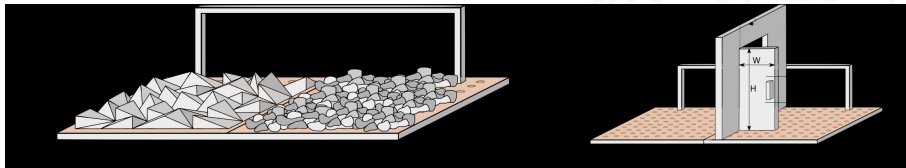
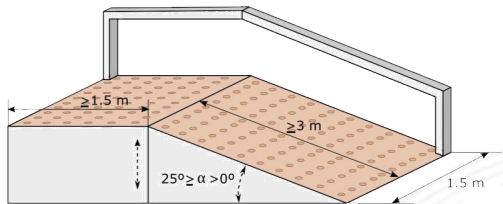
Motor skills*



www.benchmarkinglocomotion.org

* Torricelli et al. 2015, Benchmarking Bipedal Locomotion: A Unified Scheme for Humanoids, Wearable Robots, and Humans

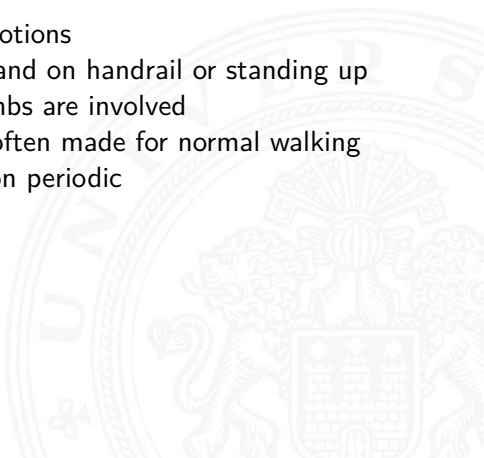
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- ▶ Small overview of full body motions
- ▶ Examples are: walking with hand on handrail or standing up
- ▶ Higher complexity since all limbs are involved
- ▶ Breaks assumptions that are often made for normal walking
- ▶ Motions can be periodic or non periodic





- ▶ Using handrail, pushing cart, opening door, holding hands, using walking stick, collaborative carrying
- ▶ Introduces additional forces on the robot
- ▶ Support polygon maybe totally different
- ▶ More complex models have to be used
- ▶ Currently mostly used approach: quadratic programming
 - ▶ Solve problem of optimizing a quadratic function with multiple linear constrains
 - ▶ Use rigid body dynamics together with a model
 - ▶ Problems
 - ▶ Model is not perfect
 - ▶ If caring an object, you need a model of it
 - ▶ Robot is maybe not perfectly rigid



- ▶ Simpler due to known start and end
- ▶ Examples
 - ▶ Standing up
 - ▶ Kicking
 - ▶ Grasping
 - ▶ Waving

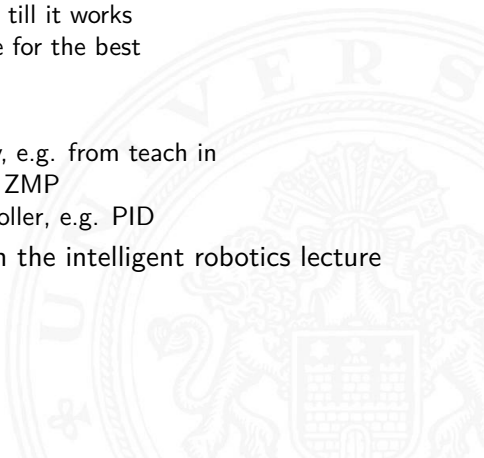




- ▶ Keypoint teach in
 - ▶ Put robot into key positions manually
 - ▶ Save joint positions at these points
 - ▶ Interpolate
 - ▶ Useful for simple motions (e.g. waving) or static robots
- ▶ Learning from demonstration
 - ▶ Either demonstrate on the robot itself or by using motion capture
 - ▶ Normally more than one demonstration
 - ▶ Not just simply replaying
- ▶ Cartesian splines
 - ▶ Define trajectories of the limbs with Cartesian splines manually
 - ▶ Comparably easy to do for humans (much better than joint space)
 - ▶ Splines configurable with few parameters
 - ▶ Use inverse kinematics to compute joint goals
 - ▶ Optionally use additional goals in the IK solver to keep balance



- ▶ DeepLearning
 - ▶ Just let it learn in simulation till it works
 - ▶ Put it on the robot and hope for the best
 - ▶ Reality gap
- ▶ Control Theory
 - ▶ Have an open loop trajectory, e.g. from teach in
 - ▶ Use a stability criterion, e.g. ZMP
 - ▶ Adjust joint goals with controller, e.g. PID
- ▶ More on the learning aspect in the intelligent robotics lecture





Questions?



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