



# Introduction to Robotics

## Lecture 9

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Technical Aspects of Multimodal Systems

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# Outline

Robot Control

Introduction to Robotics

Introduction

Coordinate systems

Kinematic Equations

Robot Description

Inverse Kinematics for Manipulators

Differential motion with homogeneous transformations

Jacobian

Trajectory planning

Trajectory generation

Dynamics

Principles of Walking

Robot Control

Introduction



# Outline (cont.)

Classification of Robot Arm Controllers

Internal Sensors of Robots

Control System of a Robot

Task-Level Programming and Trajectory Generation

Task-level Programming and Path Planning

Task-level Programming and Path Planning

Architectures of Sensor-based Intelligent Systems

Summary

Conclusion and Outlook



## Controller

- ▶ Influences one or more physical variables
  - ▶ meet a control variable
  - ▶ reduce disturbances
- ▶ Compares actual value to reference value
  - ▶ minimize control deviation



## System

- ▶ Physical or technical construct
  - ▶ input signal – stimulus
  - ▶ output signal – response
- ▶ Transforms stimulus into response
- ▶ Symbolical illustration
  - ▶ block with marked signals
  - ▶ direction of signal effect expressed with arrows



## Input and output variables

- ▶ Change over time
  - ▶ expressed as  $u(t)$  and  $v(t)$  (dynamic system)
- ▶ Infinite number of possible variables
  - ▶ for real-world dynamic technical systems (in principle)
- ▶ Description of system behaviour based on desired application
  - ▶ using the relevant variables



Given: dynamic system (to be controlled)

- ▶ Model describing dynamic system (e.g. Jacobian)
- ▶ Input variables – control variables
  - ▶ measured values (sensor data)
- ▶ Output variables – controlled variables
  - ▶ system input (force/torque data)

Problem

- ▶ Keep control variable values constant and / or
- ▶ Follow a reference value and / or
- ▶ Minimize the influence of disturbances

# Control Problem (cont.)

Sought: controller (for dynamic system)

- ▶ Implement hardware or software controller
- ▶ Alter controlled-variables (output)
- ▶ Based on control variables (input)
- ▶ Solve the problem

# Example: Cruise Control

## Input

- ▶ Speed over ground
- ▶ Relative speed to traffic
- ▶ Distance to car in front
- ▶ Distance to car behind
- ▶ Weather conditions
- ▶ Relative position in road lane
- ▶ ...

## Output

- ▶ Throttle
- ▶ Brakes
- ▶ Steering

# Development of Control Engineering - Timeline

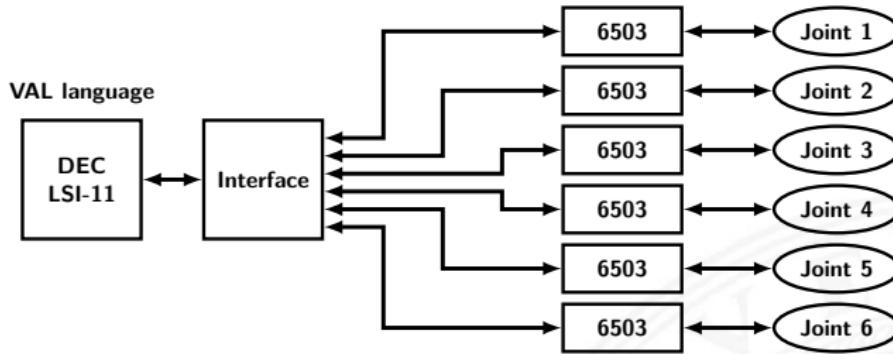
- 1788 J. Watt: engine speed governor
- 1877 J. Routh: differential equation for the description of control processes
- 1885 A. Hurwitz: stability studies
- 1932 A. Nyquist: frequency response analysis
- 1940 W. Oppelt: frequency response analysis, Control Engineering becomes an independent discipline
- 1945 H. Bode: discipline new methods for frequency response analysis
- 1950 N. Wiener: statistical methods
- 1956 L. Pontrjagin: optimal control theory, maximum principle
- 1957 R. Bellmann: dynamic programming
- 1960 direct digital control
- 1965 L. Zadeh: Fuzzy-Logic
- 1972 Microcomputer use
- 1975 Control systems for automation
- 1980 Digital device technology
- 1985 Fuzzy-controller for industrial use
- 1995 Artificial neuronal networks for industrial use

# Classification of Robot Arm Controllers

As the problem of trajectory-tracking:

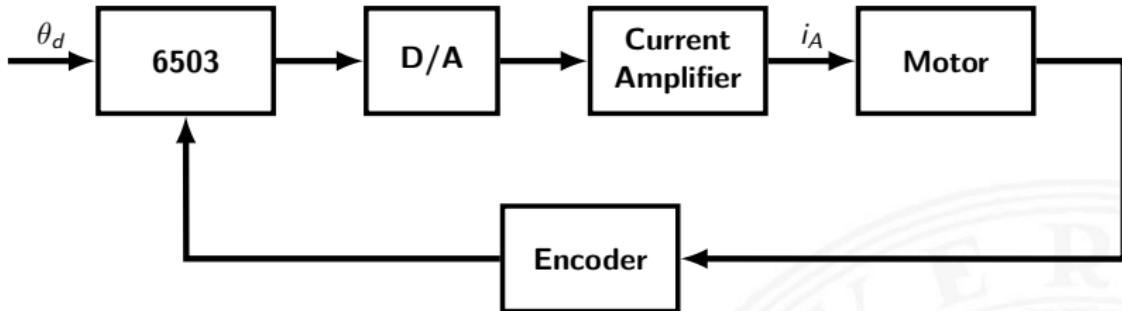
- ▶ Joint space: PID, plus model-based
- ▶ Cartesian space: joint-based
  - ▶ using kinematics or using inverse Jacobian calculation
- ▶ Adaptive: model-based adaptive control, self-tuning
  - ▶ controller (structure and parameter) adapts to the time-invariant or unknown system-behavior
  - ▶ basic control circle is superimposed by an adaptive system
  - ▶ process of adaption consists of three phases
    - ▶ identification
    - ▶ decision-process
    - ▶ modification
- ▶ Hybrid force and position control is still a current research topic

# Control System Architecture of PUMA-Robot



- ▶ two-level hierarchical structure of control system
- ▶ *DEC LSI-11* sends joint values at 35.7 Hz (28 ms)
  - ▶ trajectory
- ▶ Distance of actual value to goal value is interpolated
  - ▶ using 8,16,**32** or 64 increments

# Control System Architecture of PUMA-Robot (cont.)



- ▶ The joint control loop operates at 1143 Hz (0.875 ms)
- ▶ Encoders are used as position sensors
- ▶ Potentiometer are used for rough estimation (only PUMA-560)
- ▶ No dedicated speedometer
  - ▶ velocity is calculated as the difference of joint positions over time

# Internal Sensors of Robots

- ▶ Placed inside the robot
- ▶ Monitor the internal state of the robot
  - ▶ e.g. position and velocity of a joint

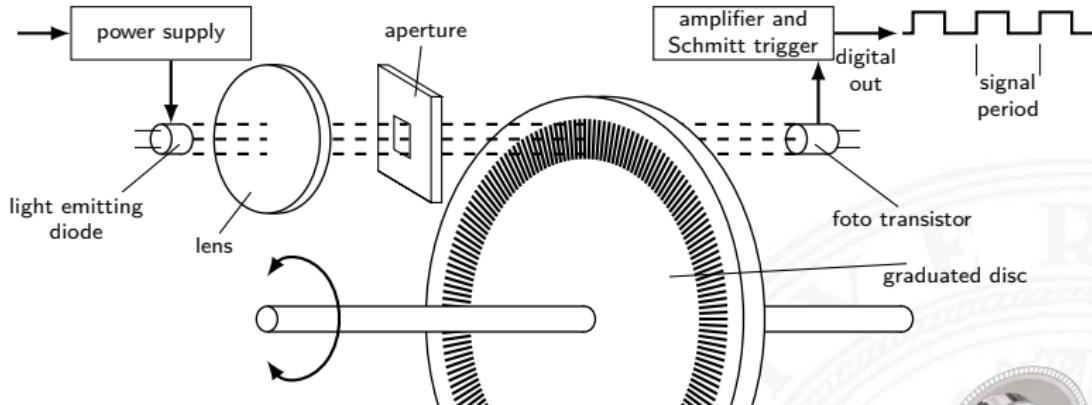
## Position measurement systems

- ▶ Potentiometer
- ▶ Incremental/absolute encoder
- ▶ Resolver

## Velocity measurement systems

- ▶ Speedometers
- ▶ Calculate from position change over time

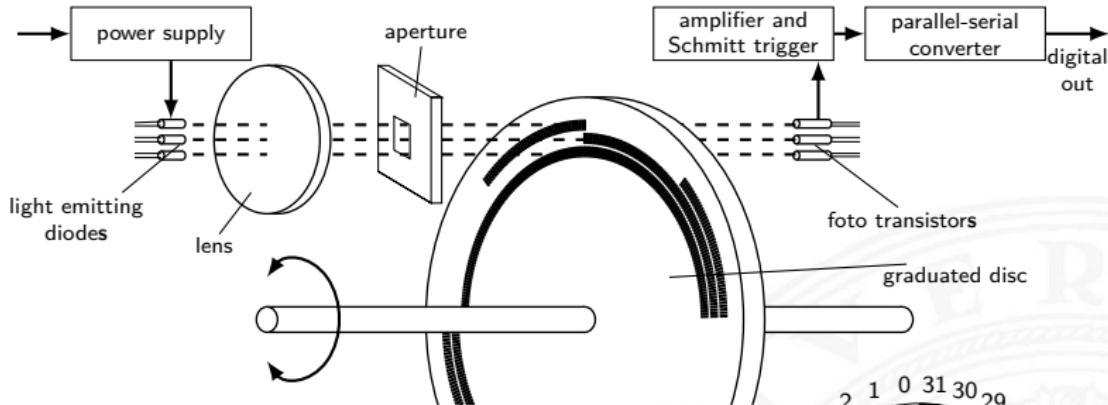
# Optical Incremental Encoders



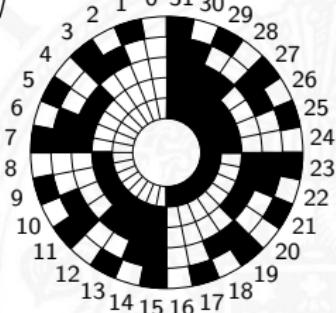
- ▶ An optical encoder reads the lines
- ▶ The disc is mounted to the shaft of the joint motor
  - ▶ PUMA-560: 1:1 ratio; .0001 rad/bit accuracy
- ▶ one special line is marked as the “zero-position”



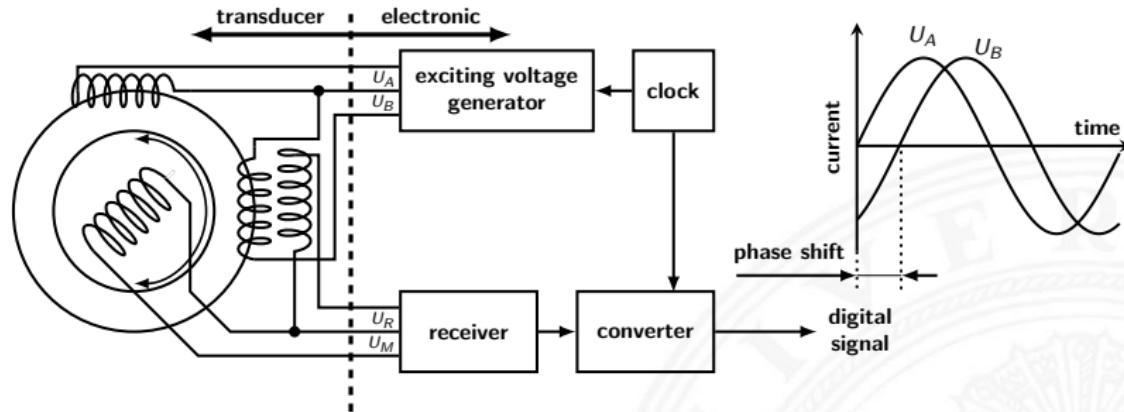
# Optical Absolute Encoder



- ▶ multiple LEDs and foto transistors
- ▶ e.g. 5 bit dual code gives 32 angular positions and  $11.25^\circ$  resolution
- ▶ parallel-serial converter required
- ▶ absolute positioning and direction encoding

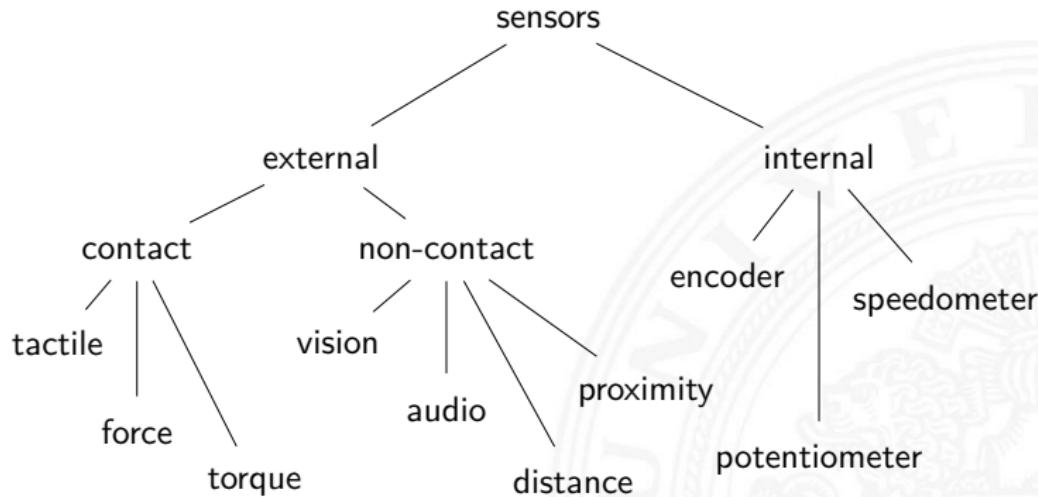


# Resolver

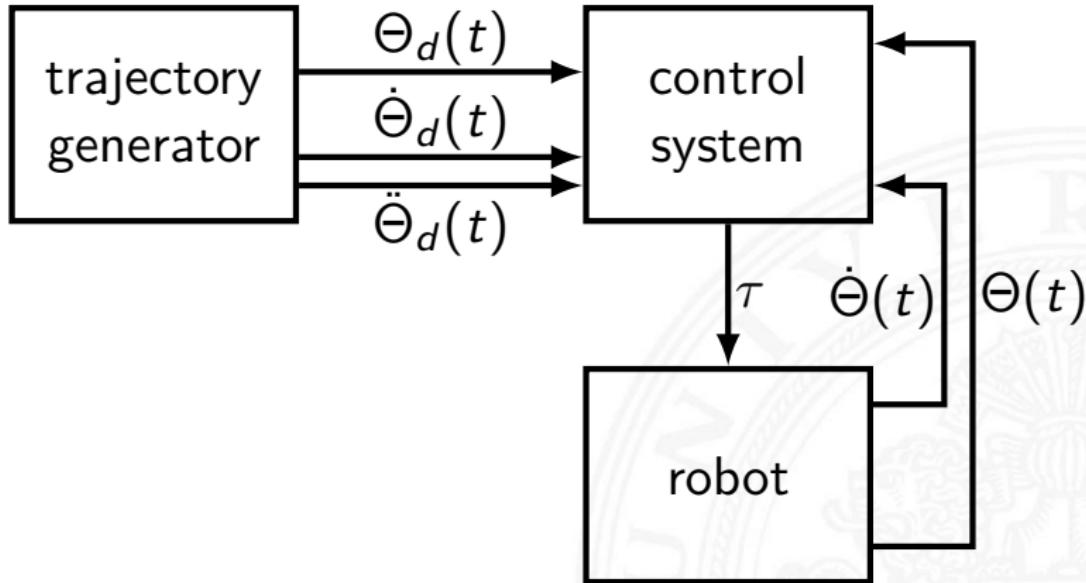


- ▶ analog rotation encoding
- ▶ phase shift between  $U_A$  and  $U_B$  determines rotation
- ▶ precision depending on digital converter

# Sensor Classification Hierarchy



# Control System of a Robot



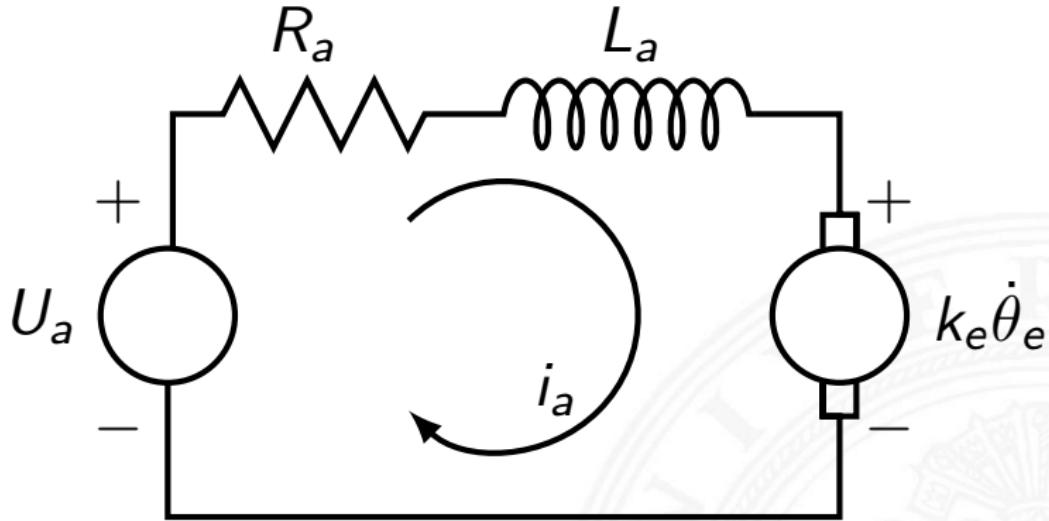


# Control System of a Robot (cont.)

- ▶ Target values
  - ▶  $\Theta_d(t)$
  - ▶  $\dot{\Theta}_d(t)$
  - ▶  $\ddot{\Theta}_d(t)$
- ▶ Magnitude of error
  - ▶  $E = \Theta_d - \Theta, \dot{E} = \dot{\Theta}_d - \dot{\Theta}$
- ▶ Output (Control) value
  - ▶  $\Theta(t)$
  - ▶  $\dot{\Theta}(t)$
- ▶ Controlled value
  - ▶  $\tau$



# Simplified Circuit of a DC-Motor



$U_a$  input voltage of armature (motor) circuit

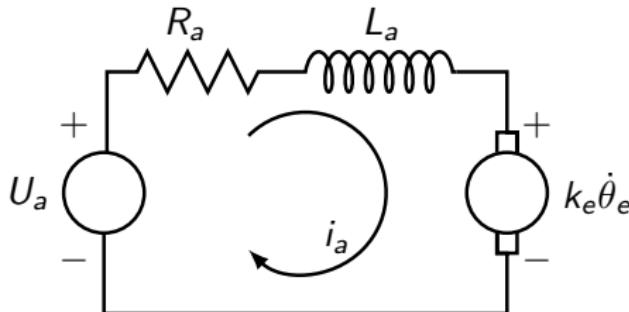
$R_a$  armature (motor) resistance

$L_a$  armature (coil) inductance

$i_a$  armature current (passing the motor)

$k_e$  exciter (motor) torque constant

# Simplified Circuit of a DC-Motor (cont.)



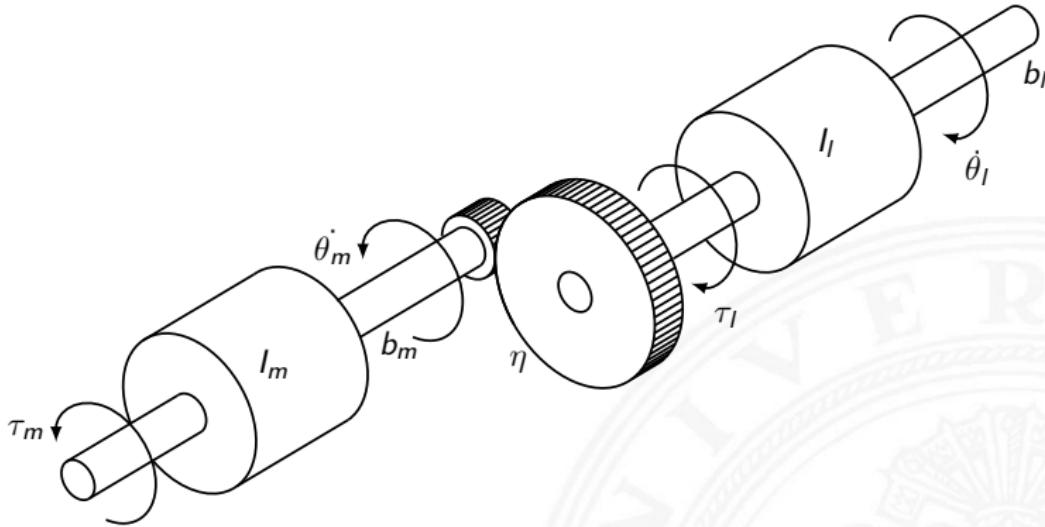
$U_a$	input voltage
$R_a$	armature resistance
$L_a$	armature inductance
$i_a$	armature current
$k_e$	exciter torque constant

The circuit can be described with the first order differential equation:

$$L_a \dot{i}_a + R_a i_a = U_a - k_e \dot{\theta}_e$$

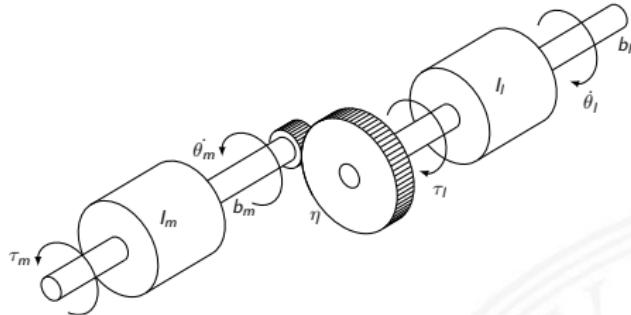
- ▶ Inductance relative to current change
- ▶ Resistance relative to absolute current
- ▶ Torque relative to rotation change

# Connection Between Motor and a Joint



- $\eta$  transmission ratio
- $I_{m/l}$  inertia of motor/load
- $\tau_{m/l}$  torque of motor/load
- $\dot{\theta}_{m/l}$  rotation velocity of motor/load
- $b_{m/l}$  friction factor

# Connection Between Motor and a Joint (cont.)



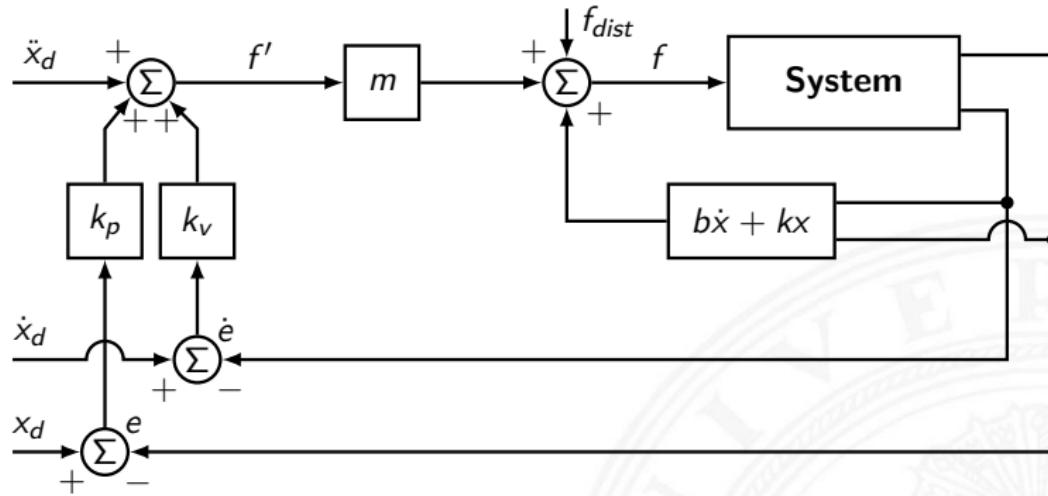
The motor torque formula is

$$\tau_m = (I_m + I_I/\eta^2)\ddot{\theta}_m + (b_m + b_I/\eta^2)\dot{\theta}_m$$

and the load torque is

$$\tau_I = (I_I + \eta^2 I_m)\ddot{\theta}_I + (b_I + \eta^2 b_m)\dot{\theta}_I$$

# Linear Control for Trajectory Tracking



$$f' = \ddot{x}_d + k_v \dot{e} + k_p e + k_i \int e dt \quad (86)$$

is called the principle of PID-control.



# PID-Controller

P Proportional controller:  $\tau(t) = k_p \cdot e(t)$

The amplification factor  $k_p$  defines the sensitivity.

I Integral controller:  $\tau(t) = k_i \cdot \int_{t_0}^t e(t') dt'$

Long term errors will sum up.

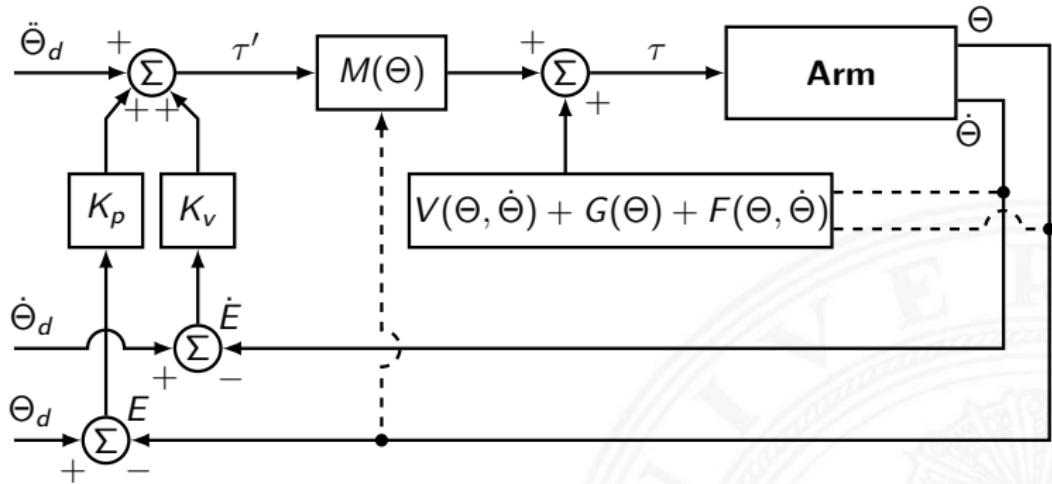
D Derivative controller:  $\tau(t) = k_v \cdot \dot{e}(t)$

This controller is sensitive to changes in the deviation.

Combined  $\Rightarrow$  PID-controller:

$$\tau(t) = k_p \cdot e(t) + k_v \cdot \dot{e}(t) + k_i \int_{t_0}^t e(t') dt'$$

# Model-Based Control for Trajectory Tracking



The dynamic equation:

$$\tau = M(\Theta)\ddot{\Theta} + V(\Theta, \dot{\Theta}) + G(\Theta)$$

where  $M(\Theta)$  is the position-dependent  $n \times n$ -mass matrix of the manipulator,  $V(\Theta, \dot{\Theta})$  is a  $n \times 1$ -vector of centripetal and Coriolis factors, and  $G(\Theta)$  is a complex function of  $\Theta$ , the position of all joints of the manipulator.

## Scientific Research

- ▶ model-based control
- ▶ adaptive control

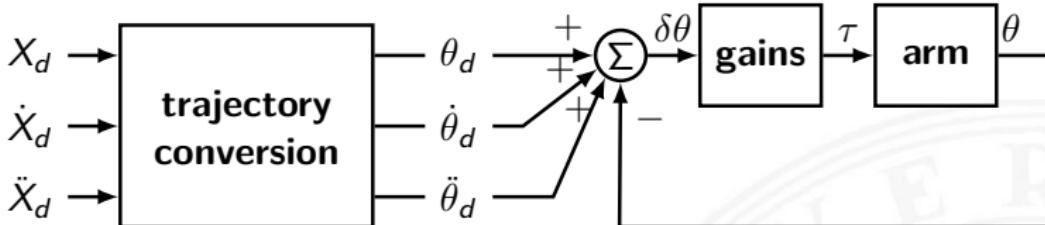
## Industrial robots

- ▶ PID-control system with gravity compensation

$$\tau = \dot{\Theta}_d + K_v \dot{E} + K_p E + K_i \int E dt + \hat{G}(\Theta)$$

# Control in Cartesian Space – Method I

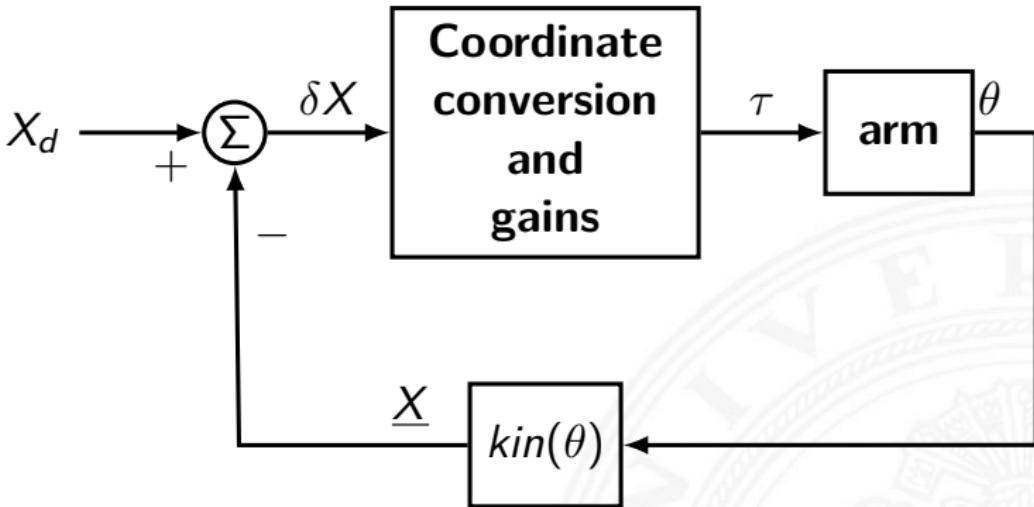
## Joint-based control with Cartesian trajectory input



- ▶ cartesian trajectory is converted into joint space first
- ▶ joint space trajectory is sent to the controller
- ▶ trajectory controller sends joint targets to motor controllers
- ▶ motor controller sends torque data to motor
- ▶ sensors output joint state

# Control in Cartesian Space – Method II

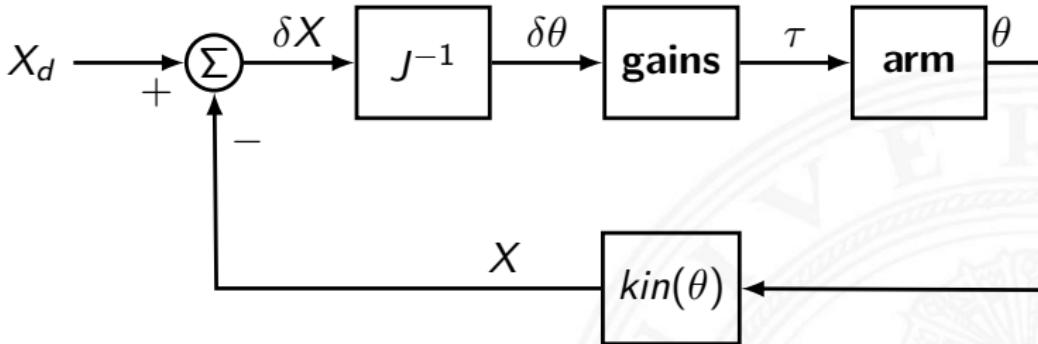
Cartesian control via calculation of kinematics



- ▶ controller operates in cartesian space
- ▶ joint space conversion within control cycle
- ▶ error values in cartesian space using FK

# Control in Cartesian Space – Method III

Cartesian control via calculation of inverse Jacobian



- ▶ no explicit joint space conversion
- ▶ dynamic conversion using inverse Jacobian

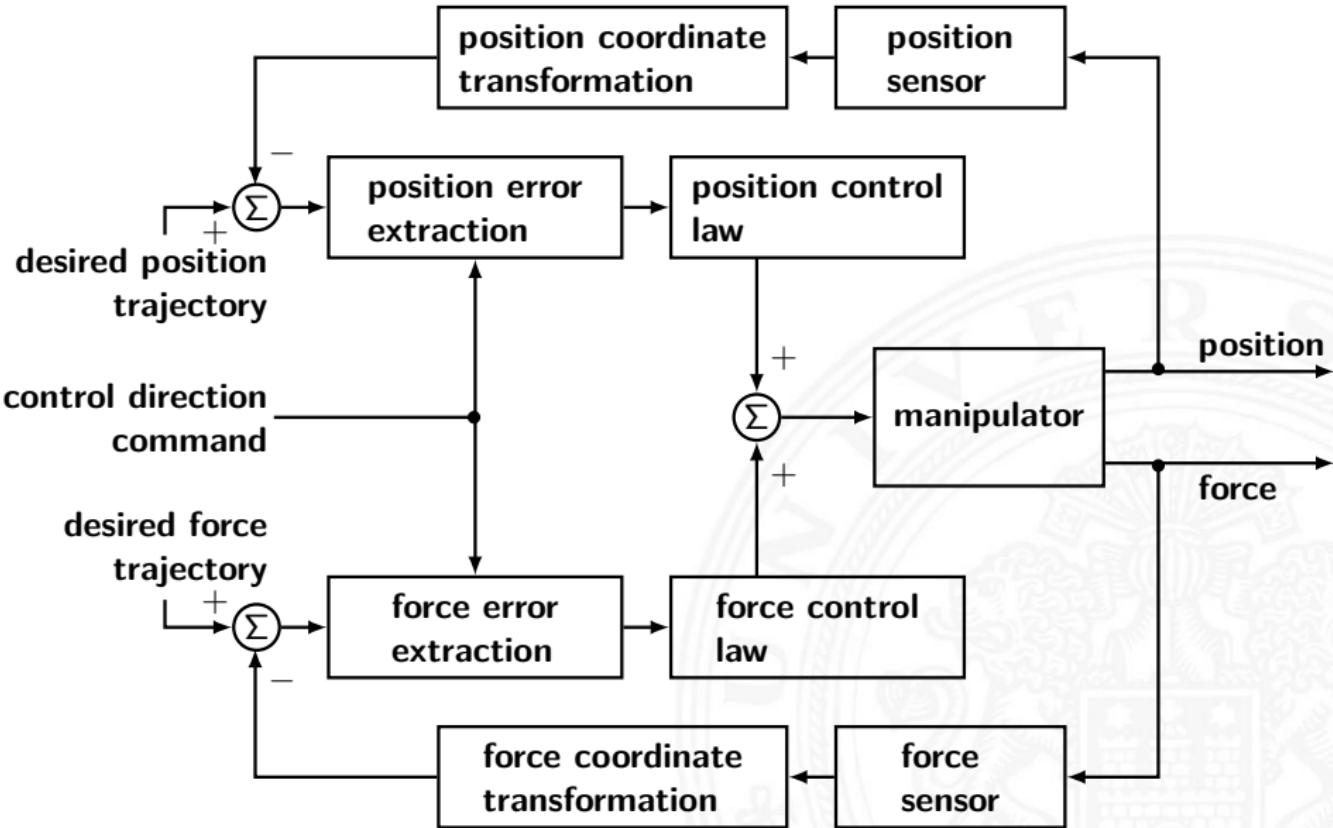
## Motivation

Certain tasks require control of both: position and force of the end-effector:

- ▶ assembly
- ▶ grinding
- ▶ opening/closing doors
- ▶ crank winding
- ▶ ...

An example shows two feedback loops for separate control of position and force

# Hybrid Control of Force and Position (cont.)





# Hybrid Force/Torque Control for safe HRI

Robot Control - Control System of a Robot

Introduction to Robotics





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