

Technical Aspects of Multimodal Systems Department of Informatics

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Introduction to Robotics Assignment #1

Due: 11.05.2020, 23:59

Task 1.1 (8 points) Pyramid: A pyramid (square base $AB = BC = CD = DA = 42\,mm$; plumbline $ME = 12\,mm$, with vertex E located at the top and point M located at the center of the base) is held by a robot so that its square base ABCD is located in the xy-plane of a cartesian world coordinate frame M_{xyz} , with point M at its origin, the edges AB and CD parallel to the x-axis and the edged BC and AD parallel to the y-axis. Attached to the pyramid is an object coordinate frame M_{uvw} , which initially coincides with M_{xyz} . Write down the general formula for each rotation.

- 1.1.1 (4 points): Determine the locations of the vertices A through E, after the following sequence of rotations has been performed by the robot:
 - 1. Rotation by $\psi = 50^{\circ}$ around M_w
 - 2. Rotation by $\varphi=-35^\circ$ around M_u
 - 3. Rotation by $\theta=340^\circ$ around M_v
- 1.1.2 (4 points): Same sequence of rotations, but using the rotation axes M_z , M_x and M_y instead.

Task 1.2 (6 points) Homogeneous transformations: Given are three frames A, B and C as well as the following two homogeneous transformations:

$$^{A}T_{B} = \begin{bmatrix} 1/\sqrt{2} & 1/\sqrt{2} & 0 & 1 \\ -1/\sqrt{2} & 1/\sqrt{2} & 0 & 1 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

and

$${}^{B}T_{C} = \begin{bmatrix} \sqrt{3}/2 & -1/2 & 0 & 2\\ 1/2 & \sqrt{3}/2 & 0 & 1\\ 0 & 0 & 1 & 0\\ 0 & 0 & 0 & 1 \end{bmatrix}$$

- **1.2.1 (3 points):** Can the interpretation of the transformation AT_C be considered to be unambiguous? Explain your answer.
- 1.2.2 (3 points): Visualize the three coordinate systems with a tool of your choice.

Task 1.3 (6 points) Euler angles:

- **1.3.1 (4 points):** Give four examples of Euler angle combinations (φ, θ, ψ) and interpret their geometric meaning using natural language.
- "This is a rotation around x by φ " is not sufficient. Explain the properties of the transformation.
- **1.3.2 (2 points):** There are 12 possible sequences of rotations with Euler-angles around the axes (see slide 29). Explain why there are exactly 12!