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TossingBot: Learning to Throw Arbitrary Objects with Residual Physics

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Technical Aspects of Multimodal Systems

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What robots can do

- ▶ Pick (Grasp)
- ▶ Place
- ▶ Move
- ▶ Push
- ▶ Interact with humans
- ▶ ...

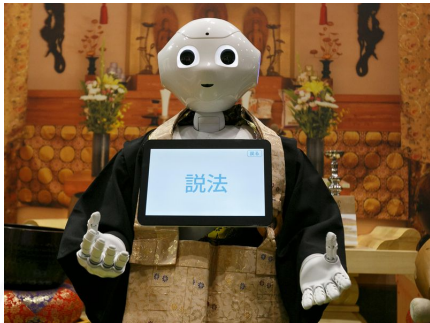


Figure: Robot conducting Buddhist funeral [Mat]

[SK16]

... and toss

- ▶ Zheng et al. presented TossingBot in 2019
- ▶ End-to-end formalism for grasping and throwing
- ▶ Deployed to an UR5 robot

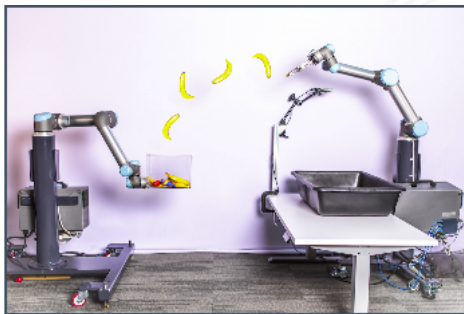


Figure: UR5 throws a banana [Zen19]

Paper:

TossingBot: Learning to Throw Arbitrary Objects with Residual Physics [Zen+19]

- ▶ Developed at *Google AI* and the *Princeton University*
- ▶ by Andy Zhang
- ▶ Other contributors from Columbia University and the MIT
- ▶ Best Systems Paper Award, Robotics Science and Systems (2019)

Characteristics:

- ▶ (Self-) supervised learning
- ▶ Trial and error learning
- ▶ Main components:
 - ▶ Deep Neural Networks
 - ▶ Physics controller
- ▶ Key aspects:
 - ▶ Joint learning of grasping and throwing policies
 - ▶ Residual learning of throw release velocities

- ▶ Not the only tossing approach

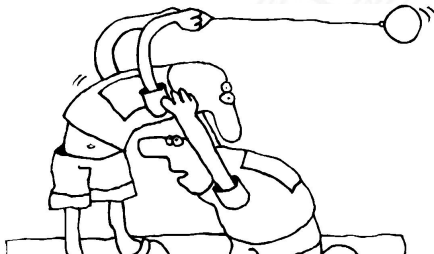
Benefits

- ▶ **Exploit dynamics** to increase robot's capabilities
- ▶ **Extends** the **operation radius**
- ▶ **Increase** the **frequency** for pick and place
- ▶ Can outperform humans

Challenges

- ▶ Acquisition of reliable **pre-throw conditions**
 - ▶ e.g grasp of the object
- ▶ Handling of **object-centric properties**
 - ▶ e.g. mass distribution, friction and shape
- ▶ and **dynamics**
 - ▶ e.g. aero-dynamics

[Gra]



Basics



Self Supervised Learning

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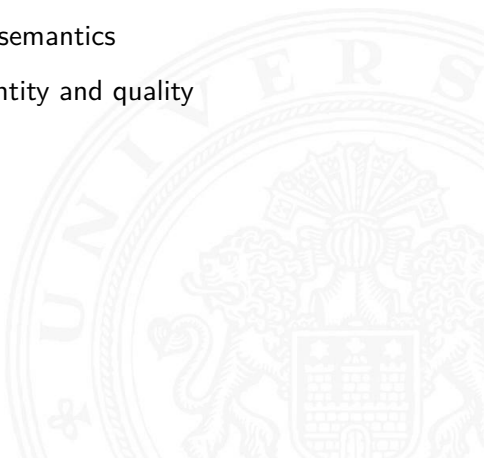
Conclusion

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Appendix

- ▶ Supervised learning example: Support Vector Machines
- ▶ Efforts manual labeling
- ▶ (Too) many possibilities for an object to grasp
- ▶ Human notions are biased by semantics
- ▶ Datasets are restricted in quantity and quality
→ overfitting

[PG16]





Self Supervised Learning (cont.)

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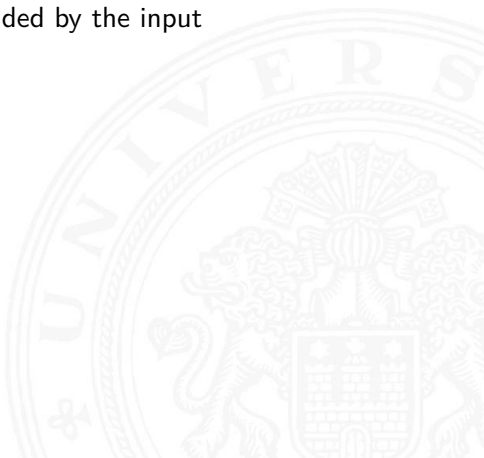
Conclusion

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Appendix

- ▶ Self-supervised learning tends to limit human involvement
- ▶ Task is framed into special form to predict only subset of information
- ▶ All information has been provided by the input
- ▶ Self-generating its labels

[PG16; Wen19]



Self Supervised Learning (cont.)

- ▶ Trial and error training obtains ground truth labels y_i and $\bar{\delta}_i$
- ▶ At each training step a visual input is fed into the network
- ▶ Grasping and throwing parameters are predicted
- ▶ Ground truth grasp success label y_i generated either
 - ▶ by gripper distance threshold or
 - ▶ by throwing success (target hit)

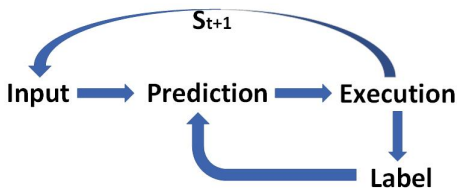


Figure: Training circle

Self Supervised Learning (cont.)

- ▶ After throw the landing location is measured
- ▶ Landing location p and release velocity v is sampled
- ▶ Ground truth residual label $\bar{\delta}_i$ is obtained by $\|v_{x,y}\| - \|\hat{v}_{x,y}\|_{\bar{p}}$
- ▶ Training environment is independently reset by the robot



Figure: Reset training environment [Zen19]

Joint Learning of Policies

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- ▶ DNN¹ maps from visual observations to control parameters:
 - ▶ Likelihood of grasping success
 - ▶ Throwing release velocities
- ▶ Grasping directly supervised by throw accuracy
- ▶ Throws directly conditioned on specific grasps
- ▶ Stable grasps \iff predictable throws and throwing velocities

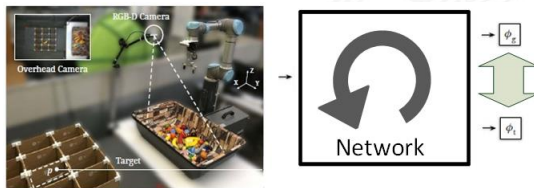


Figure: DNN black box [Zen+19]

¹Deep Neural Network

Learning of release velocities

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- ▶ Physics controller predict throw velocities \hat{v}
- ▶ Based on ideal ballistic motion
- ▶ Residual δ is (learned) corrective factor
- ▶ Final release velocity: $v = \hat{v} + \delta$

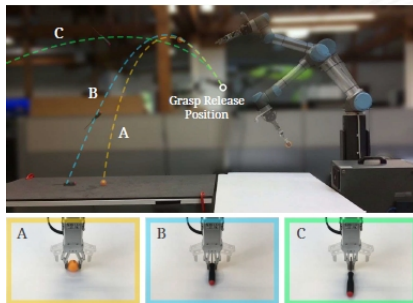


Figure: Different projectile trajectories [Zen+19]

Methods

- ▶ Neural Network: $f(I, p)$ ²
- ▶ Output: Prediction of parameters ϕ_g and ϕ_t
- ▶ Parameters used by grasping and throwing motion primitives
- ▶ Objective: Optimize parameter prediction for a hit

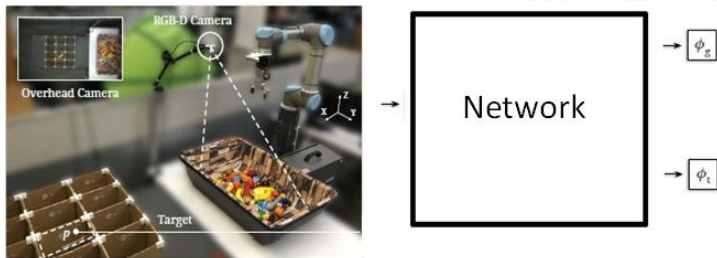


Figure: DNN black box [Zen+19]

² I = visual observation, p = landing location

Perception Module

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- ▶ Input: RGB-D heightmap I
- ▶ Output: Spatial feature representation μ
- ▶ Used by grasping and throwing module

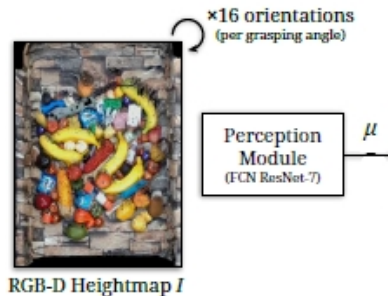


Figure: Input to perception module [Zen+19]

Grasping Module

- ▶ Outputs a probability map Q_g (grasping scores)
- ▶ Each pixel value represents probability of grasping success
- ▶ Input heightmap is rotated 16 x
- ▶ Pixel with highest probability determine ϕ_g
- ▶ Grasping primitive takes $\phi_g = (x, \theta)$
where x = pixel location, θ = rotation angle

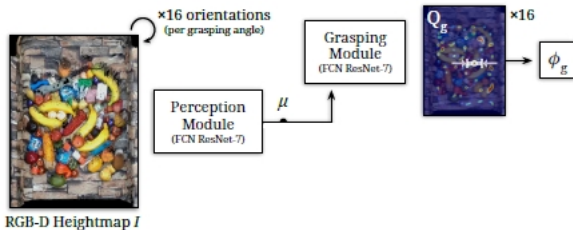


Figure: Grasping module [Zen+19]

Throwing Process

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- ▶ Predict release position r of throwing primitive
 - ▶ Distance $\sqrt{r_x^2 + r_y^2}$ for point of release to base is fixed
- ▶ Predict release velocity v of throwing primitive
 - ▶ Throw release angle θ constrained to 45°
 - ▶ Only $\|v_{x,y}\|$ is unknown

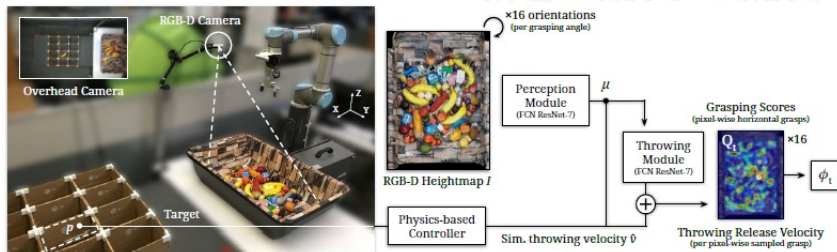


Figure: Throwing process [Zen+19]

Physics-Based Controller

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- ▶ Physic based controller predicts $\|\hat{v}_{x,y}\|$
- ▶ Assume a grasp on the center of mass of the object
- ▶ Analytically solves back for \hat{v} given p and r

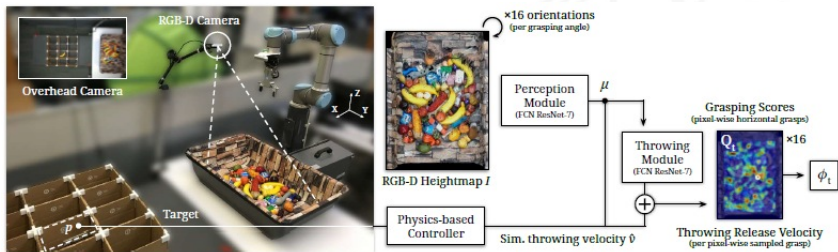


Figure: Throwing process [Zen+19]

Throwing Module

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- ▶ Output is an image Q_t
- ▶ Each pixel holds prediction for residual value δ_i
- ▶ δ_i added on top of $\|\hat{v}_{x,y}\|$
- ▶ Final release velocity: $\|v_{x,y}\| = \|\hat{v}_{x,y}\| + \delta$
- ▶ Throwing primitive takes $\phi_t = (r, v)$

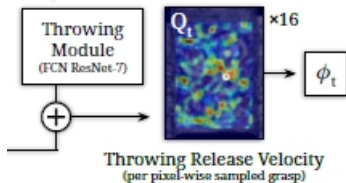


Figure: Throwing module [Zen+19]

Conditioning

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- ▶ Release velocity \hat{v} is also feed in the grasping and throwing network
- ▶ μ concatenated with k-channel image where each pixel holds value of \hat{v}
- ▶ Conditions the grasping and throwing predictions on \hat{v}
- ▶ Supervising grasps by accuracy of throws leads to better grasps

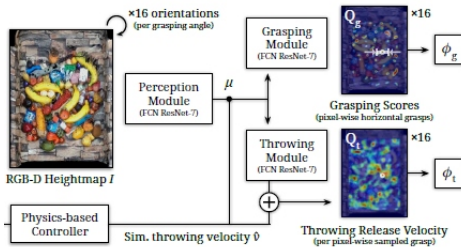


Figure: Release velocity feed [Zen+19]



- ▶ Self-supervision from trial and error
- ▶ Tracking ground truth landing position of thrown objects
- ▶ Not a single network that maps states to actions
- ▶ Four modules that provide intermediate (differentiable) results
- ▶ Output are factors that does not directly control the actuator
- ▶ Complex systems are hard to control

[Gla17]

Full Network (cont.)

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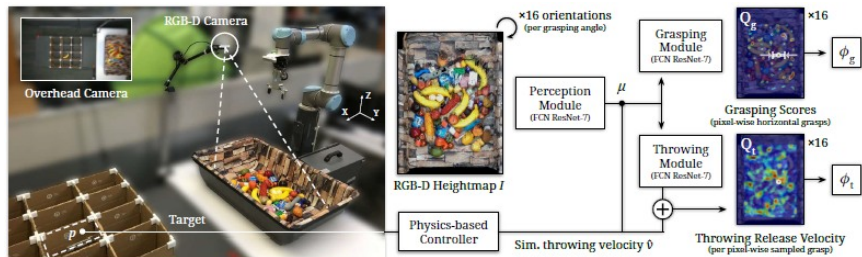


Figure: Overview [Zen+19]

Results

Experimental Setup

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- ▶ Evaluation metrics
 - ▶ Grasping success (% rate of successful grasps)
 - ▶ Throwing success (% rate of target hits)
- ▶ 12 various objects are grasped and thrown
- ▶ Target are 12 boxes outside kinematic range
- ▶ Real world: UR5 robot with RG2 gripper

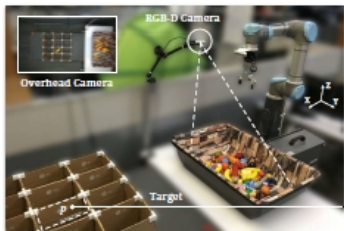


Figure: Workspace [Zen+19]



Figure: RG2 gripper [Onr]

- ▶ 8 different objects (4 seen, 4 unseen), 12 in total
- ▶ Varying center of mass (CoM)
- ▶ Simulated environment does not account for aerodynamics
- ▶ Real world experiments are conducted

TABLE I
THROWING PERFORMANCE IN SIMULATION (MEAN %)

Method	Balls	Cubes	Rods	Hammers	Seen	Unseen
Regression	70.9	48.8	37.5	32.8	41.8	28.4
Regression-PoP	96.1	73.5	52.8	47.8	56.2	35.0
Physics-only	98.6	83.5	77.2	70.4	82.6	50.0
Residual-physics	99.6	86.3	86.4	81.2	88.6	66.5

TABLE II
GRASPING PERFORMANCE IN SIMULATION (MEAN %)

Method	Balls	Cubes	Rods	Hammers	Seen	Unseen
Regression	99.4	99.2	89.0	87.8	95.6	69.4
Regression-PoP	99.2	98.0	89.8	87.0	96.4	70.6
Physics-only	99.4	99.2	87.6	85.2	96.6	64.0
Residual-physics	98.8	99.2	89.2	84.8	96.0	74.6

Figure: [Zen+19]

- ▶ 15,000 steps training, 1,000 steps testing
- ▶ Average grasping and throwing success rates

TABLE III
GRASPING AND THROWING PERFORMANCE IN REAL (MEAN %)

Method	Grasping		Throwing	
	Seen	Unseen	Seen	Unseen
Human-baseline	-	-	-	80.1±10.8
Regression-PoP	83.4	75.6	54.2	52.0
Physics-only	85.7	76.4	61.3	58.5
Residual-physics	86.9	73.2	84.7	82.3

TABLE IV
PICKING SPEED VS STATE-OF-THE-ART SYSTEMS

System	Mean Picks Per Hour (MPPH)
Cartman [24]	120
Dex-Net 2.0 [26]	250
FC-GQ-CNN [27]	296
Dex-Net 4.0 [21]	312
TossingBot (w/ Placing)	432
TossingBot (w/ Throwing)	514

Figure: [Zen+19]

- ▶ Residual physics outperforms by learning residual throwing velocities
- ▶ Compensate for for grasping offsets from objects CoM

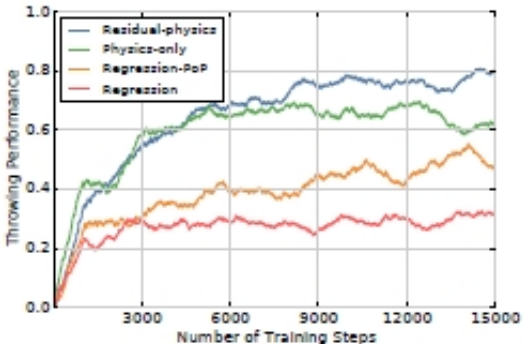


Figure: Throwing performance on hammers[Zen+19]

- ▶ 2 variants of grasp success label y_i
- ▶ Grasping supervised by throwing yields best throwing results
- ▶ Supervised grasps are more restricted, resulting in more dexterous throws

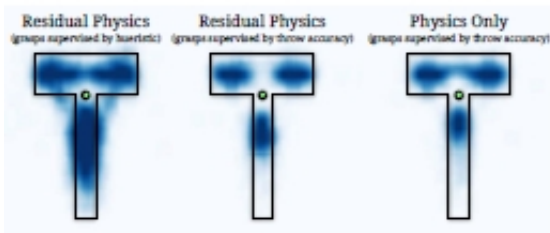


Figure: Histograms of succesfull grasps[Zen+19]

Conclusion



- ▶ Paper provides new perspectives on throwing
 - ▶ Relationship of throwing to grasping
 - ▶ Throwing correlates with grasp quality
 - ▶ Learning by combining physics with trial and error
 - ▶ Synergies between grasping and throwing is exploited
- ▶ *Residual Physics* leverage advantages of physic based controllers while maintaining the capacity to account for dynamics
- ▶ Generalization via analytic models
- ▶ Data-driven residual corrects the real world projectile velocity



Thank you for your attention!

Questions?



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References (cont.)

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- [Zen19] **Andy Zeng**. *TossingBot: Learning to Throw Arbitrary Objects with Residual Physics*. 2019. URL: <https://tossingbot.cs.princeton.edu/> (Retrieved 05/23/2020).



Video



Ballistics [Zen19]



Appendix - Future Work

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- ▶ Train networks to predict motions that account for fragile objects
- ▶ Explore additional sensing modalities such as force-torque
- ▶ How should robots learn semantics of the visual world?
- ▶ Classic computer vision: predefined semantics using manually constructed class categories
- ▶ Here: Implicitly learn object-level semantics from physical interactions



Video



[Zen19]

Appendix - Loss Function

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- ▶ Loss function for network training:
 - ▶ Binary cross-entropy error \mathcal{L}_g from predictions of grasping success
 - ▶ Huber-loss \mathcal{L}_t from its regression of δ_i for throwing

$$(1) \quad \mathcal{L} = \mathcal{L}_g + y_i \mathcal{L}_t$$

$$(2) \quad \mathcal{L}_g = -(y_i \log q_i + (1 - y_i) \log(1 - q_i))$$

$$(3) \quad \mathcal{L}_t = \begin{cases} \frac{1}{2}(\delta_i - \bar{\delta}_i)^2, & \text{for } |\delta_i - \bar{\delta}_i| < 1, \\ |\delta_i - \bar{\delta}_i| - \frac{1}{2}, & \text{otherwise} \end{cases}$$

where y_i is the binary ground truth grasp success label, q_i and $\bar{\delta}_i$ are the predicted values and $\bar{\delta}_i$ is the ground truth residual label

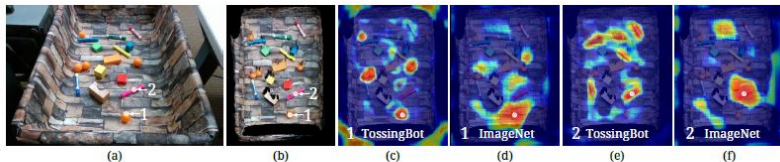


Fig. 10. **Emerging semantics from interaction.** Visualizing pixel-wise deep features μ learned by TossingBot (c,e) overlaid on the input heightmap image (b) generated from an RGB-D side-view (a) of a bin of objects. (c) shows a heatmap of pixel-wise feature distances (hotter = smaller distance) from the feature vector of a query pixel on a ping pong ball (labeled 1). Likewise, (e) shows a heatmap of pixel-wise feature distances from the feature vector of a query pixel on a pink marker pen (labeled 2). These visualizations show that TossingBot learns features that distinguish object categories from each other without explicit supervision (*i.e.*, only task-level grasping and throwing). For reference, the same visualization technique is used on deep features generated by a ResNet-18 pre-trained on ImageNet (d,f).

Figure: [Zen+19]

Appendix (cont.) - Image Projection

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- ▶ Capture RGB-D image from fixed mount camera
- ▶ Project data onto 3D-point cloud
- ▶ Orthographical back-projection in gravity direction
- ▶ color and height-from-bottom channels
- ▶ normalization allows sharing of learned convolutional filters

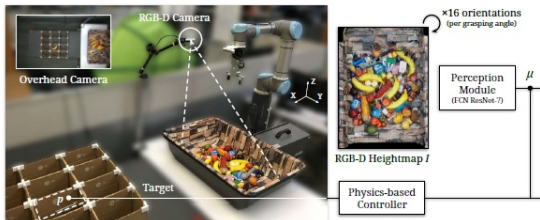


Figure: Projection [Zen+19]



Appendix (cont.) - Gripper Modalities

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- ▶ Top-down parallel yaw grasp centered at $x = (x_x, x_y, x_z)$
- ▶ Oriented θ° around gravity direction
- ▶ Gripper approaches x until middle point of finger tips meets x
- ▶ Gripper closes and lifts upwards
- ▶ Planning by stable, collision-free IK-solver



Appendix (cont.) - Release Position

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- ▶ Derive release position r from landing location p
- ▶ Assume: aerial trajectory is linear on xy -horizontal plane and in the v_x, v_y direction
- ▶ Neglect orthogonal aerodynamic forces
- ▶ Parallel aerodynamic forces are compensated
- ▶ Making all release positions accessible by robot
- ▶ Constants: $r_z = 0.04$ m and distance to base $\sqrt{r_x^2 + r_y^2} = 0.7$ m in sim, 0.02m and 0.76 m in reality
- ▶ Constraint: $(r_{x,y} - p_{x,y})xv_{x,y} = 0$



Appendix (cont.) - Physics controller

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- ▶ Physics based controller provides a closed form solution
- ▶ Generalizes well to new landing locations
- ▶ Serves as consistent approximation for \hat{v}
- ▶ Simplified model
- ▶ Neglects aerodynamic drag
- ▶ Gripper release velocity does not directly determine projectile velocity
- ▶ Centripetal forces

$$p = r + \hat{v}t + \frac{1}{2}at^2 \quad (1)$$

Appendix (cont.) Example Calculation

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- ▶ UR5 joint speed: $\frac{180^\circ}{s} \Rightarrow \omega = \frac{\pi}{s}$
- ▶ Length of lower arm: $\approx 0.49m$
- ▶ Peripheral speed: $v = \frac{\pi}{s} \cdot 0.49m \approx 1.54 \frac{m}{s}$
- ▶ Ballistic equation projectile range: $x = v_0 \cdot \cos \theta \cdot t$
- ▶ Ballistic equation ToF³: $t = \frac{2 \cdot v_0 \cdot \sin \theta}{g}$
- ▶ Throwing angle $\theta =$ impact angle $= 45^\circ$

$$x = \frac{2 \cdot (v_0)^2 \cdot \sin(2 \cdot \theta)}{2 \cdot g} = \frac{2 \cdot (1.54 \frac{m}{s})^2 \cdot \sin 90}{2 \cdot 9.81 \frac{m}{s^2}} \approx 0.24m$$

³Time-of-Flight

Ballistic calculation:

- ▶ Ballistic equation projectile range: $x = \hat{v} \cdot \cos \theta \cdot t$
- ▶ Ballistic equation ToF⁴: $t = \frac{2 \cdot v_0 \cdot \sin \theta}{g}$
- ▶ Throwing angle $\theta =$ impact angle

$$\hat{v} = \sqrt{\frac{x \cdot g}{\sin(2 \cdot \theta)}} \quad (2)$$

e.g. $\sqrt{\frac{0.24m \cdot 9.81 \frac{m}{s^2}}{\sin(2 \cdot 45)}} \approx 1.53 \frac{m}{s}$ throwing velocity



Appendix (cont.) - Learning of release velocities

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- ▶ fixed throwing release height r_z
- ▶ fixed release distance from robot base origin c_d
- ▶ release vel. angled 45° upwards
- ▶ landing location $\mathbf{p} = (p_x, p_y, p_z)$
- ▶ release position \mathbf{r} is fixed at $c_d = 0.76\text{m}$ and r_z at constant height $c_h = 0.02\text{m}$
- ▶ Release vel. magnitude $\|v\|$



Ballistic calculation:

$$\theta = \arctan\left(\frac{p_y}{p_x}\right)$$

$$r_x = c_d \sin \theta$$

$$r_y = c_d \cos \theta$$

$$\|v\| = \sqrt{\frac{a(p_x^2 + p_y^2)}{r_z - p_z - \sqrt{p_x^2 + p_y^2}}}$$



Appendix (cont.) - Self Supervised Learning

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- ▶ Pinto and Gupta [PG16] emphasized benefits of large-scale datasets
- ▶ Introduced large robot dataset
- ▶ Limit human involvement
- ▶ Execute trial and error grasps
- ▶ Image patch of grasp feed to CNN
- ▶ Output is the likelihood of the grasp

[PG16]



Appendix (cont.) - Self Supervised Learning

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- ▶ Trained model is used for next grasping stage
- ▶ Execute grasp along the predicted output
- ▶ Grasps are evaluated by gripper's force sensor
- ▶ Correct grasp modalities are reinforced

[PG16]



Appendix (cont.) - Self Supervised Learning

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- ▶ better utilizing unlabelled data, while learning in a supervised learning manner
- ▶ framing a supervised learning task in a special form to predict only a subset of information using the rest
- ▶ all the information needed, both inputs and labels, has been provided. This is known as self-supervised learning.
- ▶ self-generated labels
- ▶ To make use of this much larger amount of unlabeled data, one way is to set the learning objectives properly so as to get supervision from the data itself.
- ▶ The self-supervised task, also known as pretext task, guides us to a supervised loss function.

[Wen19]

Algorithm 1 System Pipeline

```

1: Initialize robot.
2: Initialize policy with model  $f$ .
3: Initialize replay buffer.
4: while step  $i < N$  and not terminate do
5:    $I^i = \text{robot.CaptureState}()$ 
6:    $p^i = \text{robot.SelectTarget}()$ 
7:    $\phi_g^i, \phi_t^i = f.\text{Inference}(I^i, p^i)$ 
8:   while robot.is_grasping do
9:      $f.\text{ExperienceReplay}(\text{buffer})$ 
10:   $y^{i-1} = \text{robot.CheckGraspSuccess}()$ 
11:   $\text{robot.ExecuteThrow}(\phi_t^{i-1}, p^{i-1})$       ▷ asynchronous
12:  while robot.is_throwing do
13:     $f.\text{ExperienceReplay}(\text{buffer})$ 
14:   $\text{robot.ExecuteGrasp}(\phi_g^i)$                 ▷ asynchronous
15:   $\bar{p}^{i-1} = \text{robot.TrackLanding}()$ 
16:   $\text{buffer.SaveData}(I^{i-1}, p^{i-1}, \phi_g^{i-1}, \phi_t^{i-1}, y^{i-1}, \bar{p}^{i-1})$ 
17:   $i = i + 1$ 

```

Figure: Ideal ballistic equations [Zen+19]



Ballistic Flight Equations

(no drag - no thrust)

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t = time

y = height

x = distance

V = vertical velocity

U = horizontal velocity

g = gravitational
acceleration

Weight is only
external force

Launch



Coasting
Ascent

Coasting
Descent

h

Horizontal Component:

$$U = U_0$$

$$x = U_0 t$$

Vertical Component:

$$V = V_0 - g t$$

$$y = V_0 t - .5 g t^2$$

At highest point:

$$V = 0$$

$$t = V_0 / g$$

$$h = .5 V_0^2 / g$$

At ground impact:

$$y = 0$$

$$t = 2 V_0 / g$$

$$V = -V_0$$

Figure: Ideal ballistic equations [NAS]



Vector Components

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A **vector quantity** has both **magnitude** and **direction**.

components are scalars

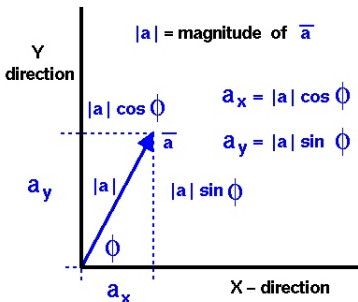


Figure: Vector components [NAS]

Appendix (cont.)

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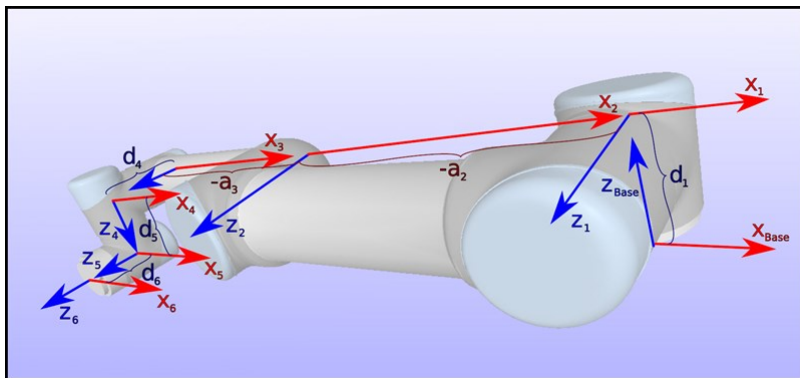


Figure: Denavit–Hartenberg parameters of UR robots [Uni18]

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UR5e							
Kinematics	theta [rad]	a [m]	d [m]	alpha [rad]	Dynamics	Mass [kg]	Center of Mass [m]
Joint 1	0	0	0.1625	$\pi/2$	Link 1	3.761	[0, -0.02561, 0.00193]
Joint 2	0	-0.425	0	0	Link 2	8.058	[0.2125, 0, 0.11336]
Joint 3	0	-0.3922	0	0	Link 3	2.846	[0.15, 0.0, 0.0265]
Joint 4	0	0	0.1333	$\pi/2$	Link 4	1.37	[0, -0.0018, 0.01634]
Joint 5	0	0	0.0997	$-\pi/2$	Link 5	1.3	[0, 0.0018, 0.01634]
Joint 6	0	0	0.0996	0	Link 6	0.365	[0, 0, -0.001159]

Figure: UR5 Technical specifications [Uni16]

Appendix (cont.)

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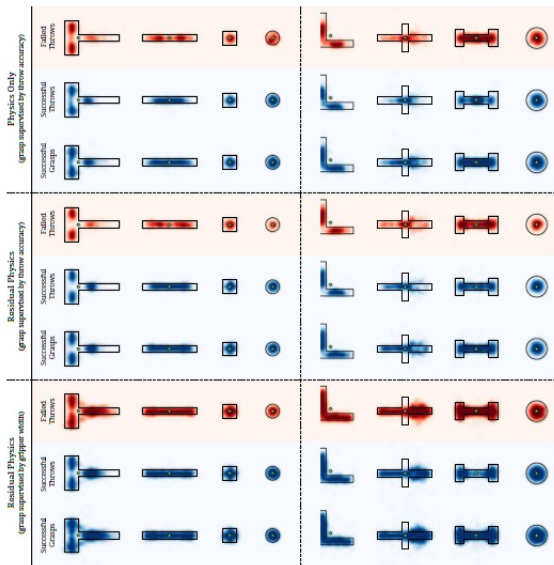
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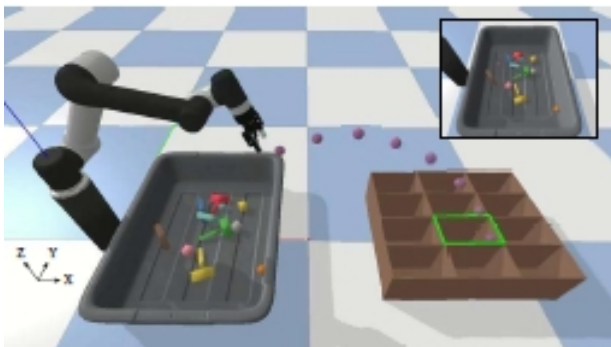
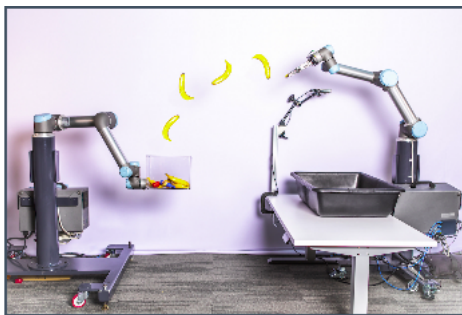


Figure: PyBullet simulation [Zen+19]



Video



[Zen19]



Video



[Zen19]