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Challenges of Humanoid Motion Planning for Navigation

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Technical Aspects of Multimodal Systems

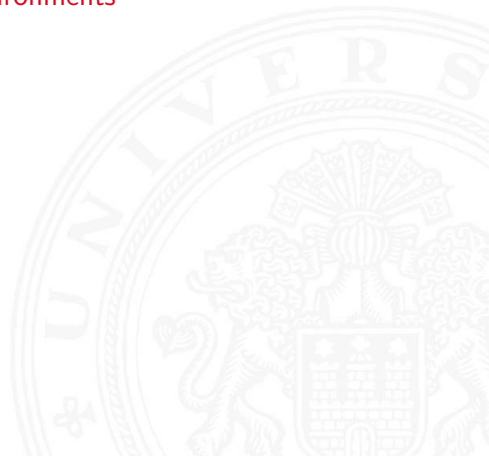
05. November 2018



Outline

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1. Introduction and Motivation
2. Dynamic Window Approach
3. Dynamic Footstep Planning
4. Footstep Planning for 3D Environments
5. Conclusion

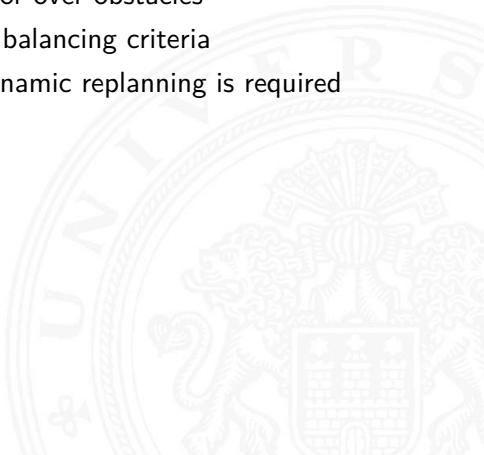




Introduction and Motivation

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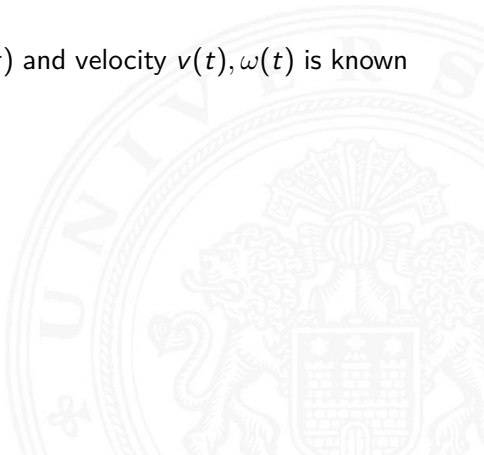
- ▶ humanoid robots are mobile robots
- ▶ approaches for traditional mobile robots (with wheels) only work for flat terrain
- ▶ humanoid robots can step on or over obstacles
- ▶ navigation space is limited by balancing criteria
- ▶ environment is dynamic → dynamic replanning is required





Dynamic Window Approach [FBT]

- ▶ global path has been computed by a standard pathfinding algorithm (A^* etc.)
- ▶ motion capabilities of the robot are known
 - ▶ velocity limits (v, ω)
 - ▶ acceleration limits $(\dot{v}, \dot{\omega})$
- ▶ current position $x(t), y(t), \theta(t)$ and velocity $v(t), \omega(t)$ is known





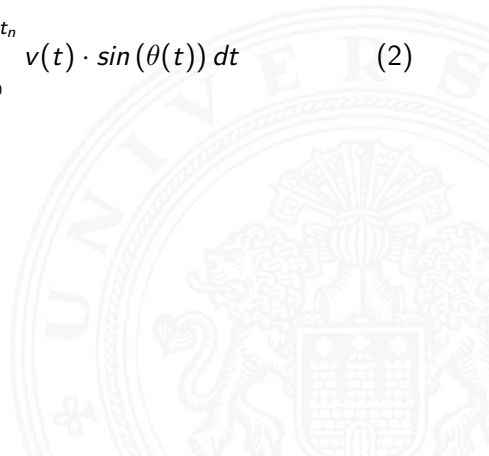
Dynamic Window Approach [FBT]

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future position can be calculated

$$x(t_n) = x(t_0) + \int_{t_0}^{t_n} v(t) \cdot \cos(\theta(t)) dt \quad (1)$$

$$y(t_n) = y(t_0) + \int_{t_0}^{t_n} v(t) \cdot \sin(\theta(t)) dt \quad (2)$$



Dynamic Window Approach [FBT]

velocities depend on current velocities $v(t), \omega(t)$ and accelerations $\dot{v}(\hat{t}), \dot{\omega}(\hat{t})$

$$x(t_n) = y(t_0) + \int_{t_0}^{t_n} \left(v(t_0) + \int_{t_0}^t \dot{v}(\hat{t}) d\hat{t} \right) \cdot \cos \left(\theta(t) + \int_{t_0}^t \left(\omega(t_0) + \int_{t_0}^{\hat{t}} \dot{\omega}(\tilde{t}) d\tilde{t} \right) d\hat{t} \right) dt \quad (3)$$

Dynamic Window Approach [FBT]

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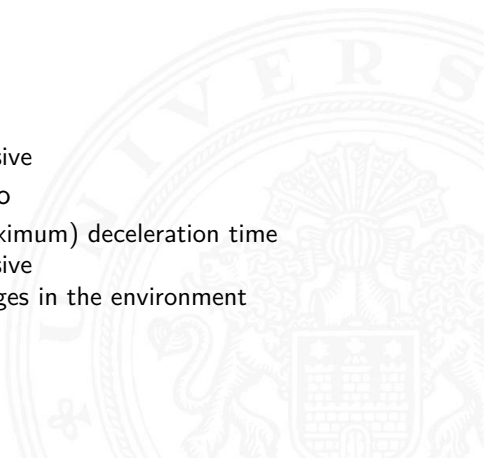
$$y(t_n) = y(t_0) + \int_{t_0}^{t_n} \left(v(t_0) + \int_{t_0}^t \dot{v}(\hat{t}) d\hat{t} \right) \cdot \sin \left(\theta(t) + \int_{t_0}^t \left(\omega(t_0) + \int_{t_0}^{\hat{t}} \dot{\omega}(\tilde{t}) d\tilde{t} \right) d\hat{t} \right) dt \quad (4)$$



Dynamic Window Approach [FBT]

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- ▶ discrete simulation of possible trajectories
- ▶ evaluation of trajectories based on
 - ▶ target heading
 - ▶ clearance
 - ▶ velocity
 - ▶ distance to path
- ▶ finer granularity leads to
 - ▶ closer to optimal solution
 - ▶ computationally more expensive
- ▶ longer simulation time leads to
 - ▶ minimum should be the (maximum) deceleration time
 - ▶ computationally more expensive
 - ▶ longer reaction time to changes in the environment





Dynamic Window Approach [FBT]

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Video Break [Tar]



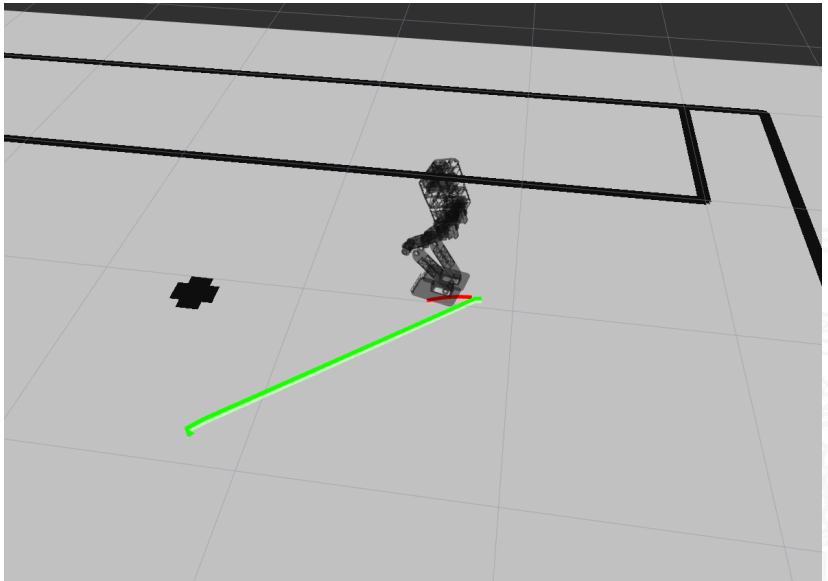


Figure 1: Visualization of local and global plan for a humanoid robot



Dynamic Window Approach [FBT]

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Video Break 2





Conclusion

- ▶ quick reactions to changes in the environment (faster than global replanning)
- ▶ computationally inexpensive
- ▶ collision free trajectory
- ▶ used in many real world robots
- ▶ planning restricted to x, y, θ



Dynamic Footstep Planner [GHB]

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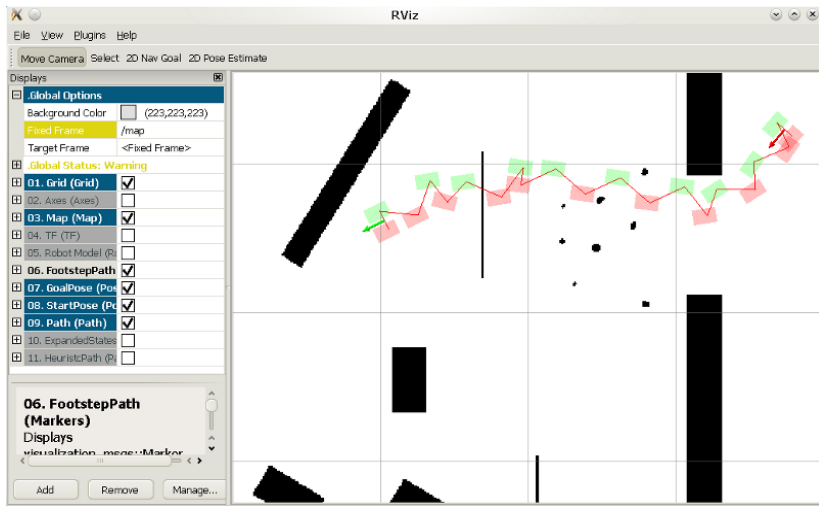


Figure 2: Visualization of planned footsteps between and above obstacles [GH]



Dynamic Footstep Planner [GHB]

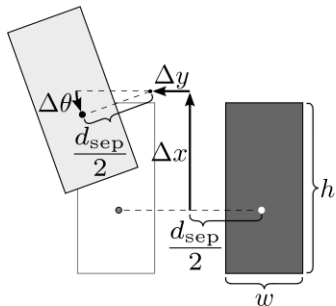
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- ▶ control feet position instead of velocities and accelerations
- ▶ walking engine needs to support this



Dynamic Footstep Planner [GHB]

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Parameter	Value / Range
d_{sep}	9.5 cm
w	9.0 cm
h	16.0 cm
Δx	$[-4.0, 4.0]$ cm
Δy	$[-1.0, 4.0]$ cm
$\Delta \theta$	$[-2.9, 20.0]^\circ$

Figure 3: possible parameters of the foot placement vector [GHB]



State is modeled as position of supporting foot:

$$s = (x, y, \theta) \quad (5)$$

State transition is modeled as taking one step:

$$a = (\Delta x, \Delta y, \Delta \theta) \quad (6)$$

Cost of state transition is modeled as:

$$c(s, s') = \|(x, y), (x', y')\| + k + d(s') \quad (7)$$

Where $\|(x, y), (x', y')\|$ is the distance travelled, k is a constant cost to minimize steps taken and $d(s')$ is distance to closest obstacle



Dynamic Footstep Planner [GHB]

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Efficient collision checking between foot and environment is necessary





Heuristic for path evaluation was chosen statistically

$$h_1 = \omega_1 \| (x, y), (x_{start}, y_{start}) \| + kS_1(s, s_{start}) \quad (8)$$

$$h_2 = \omega_1 \| (x, y), (x_{start}, y_{start}) \| + kS_1(s, s_{start}) + \omega_2 |\theta - \theta_{start}| \quad (9)$$

$$h_3 = \omega_1 \mathcal{D}(s, s_{start}) + kS_2(s, s_{start}) \quad (10)$$

With ω_1, ω_2 as scaling factors, S_1 as expected number of footsteps based on distance, k as constant cost per step, \mathcal{D} as length of 2D Path and S_2 as expected number of footsteps along \mathcal{D}

Heuristic for path evaluation was chosen statistically

$$h_1 = \omega_1 \|(x, y), (x_{start}, y_{start})\| + kS_1(s, s_{start}) \quad (8)$$

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$$h_3 = \omega_1 \mathcal{D}(s, s_{start}) + kS_2(s, s_{start}) \quad (10)$$

With ω_1, ω_2 as scaling factors, S_1 as expected number of footsteps based on distance, k as constant cost per step, \mathcal{D} as length of 2D Path and S_2 as expected number of footsteps along \mathcal{D}

h_3 was chosen through statistical evaluation

Dynamic Footstep Planner [GHB]

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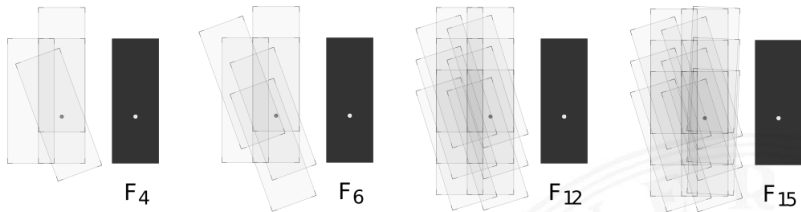


Figure 4: sets of possible foot placements [GHB]

Dynamic Footstep Planner [GHB]

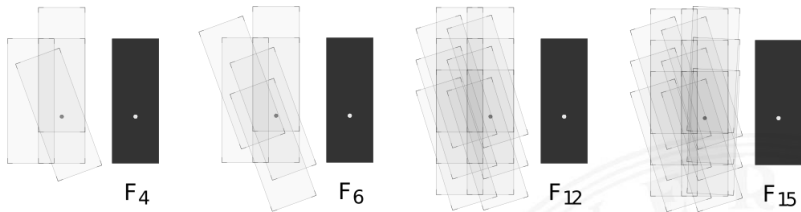


Figure 4: sets of possible foot placements [GHB]

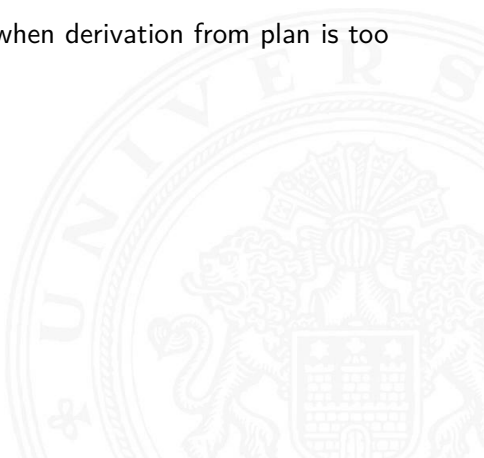
F_{12} was chosen through statistical analysis



Dynamic Footstep Planner [GHB]

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- ▶ foot slippage and inaccurate joints cause open loop execution to be infeasible
- ▶ adaptation of next step to incorporate information about current position
- ▶ efficient replanning using D^* when derivation from plan is too great





Dynamic Footstep Planner [GHB]

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- ▶ stepping over planar or near planar objects is achieved
- ▶ stepping onto objects is not achieved
- ▶ cluttered environments create local minima [HDLB]



Footstep Planning for 3D Environments [KDF⁺]

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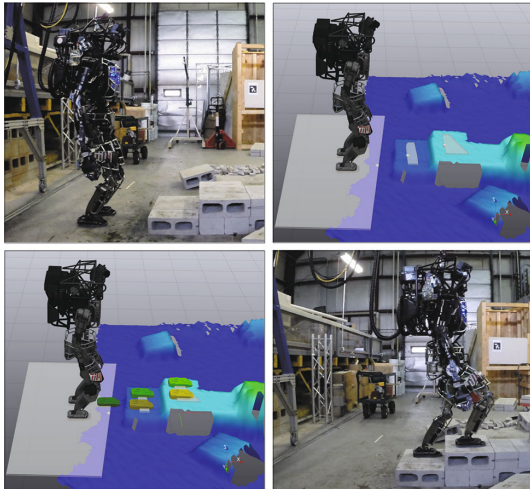


Figure 5: Planned Footsteps for climbing Stairs [KDF⁺]



Footstep Planning for 3D Environments [KDF⁺]

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- ▶ sets of footsteps limit available position
- ▶ continuous searching for complete area is
- ▶ subdivide into convex regions with convex cost function
- ▶ easily solvable by optimization



Footstep Planning for 3D Environments [KDF⁺]

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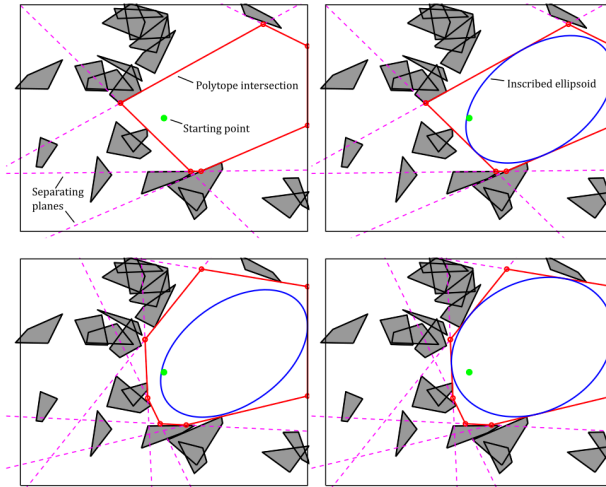


Figure 6: Convex region calculation [KDF⁺]



Footstep Planning for 3D Environments [KDF⁺]

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- ▶ trajectory of center of mass and center of pressure needs to be planned
- ▶ reaching a stable pose after the last step
- ▶ placing feet on sloped terrain is not modeled



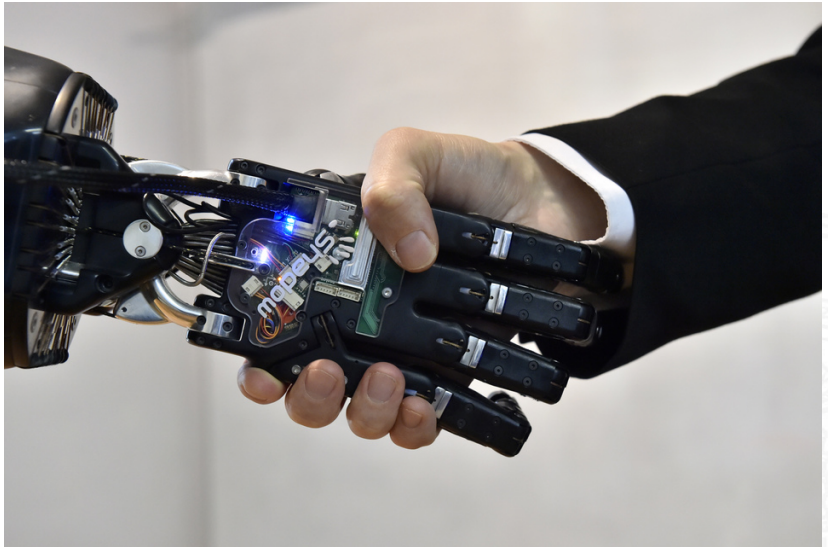


Human comparison

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Video [Cel]



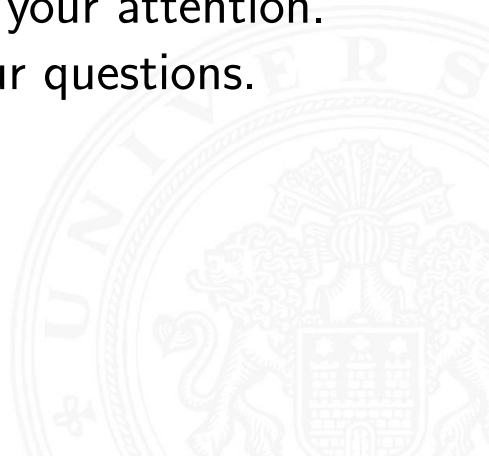


[noa]

Comparison

	DWA	Footstep Planning
dimensionality of navigation	3	3-6
computational difficulty	low	high
nav. on flat ground	yes	yes
nav. over obstacles	no	yes
stepping on obstacles	no	yes
sloped ground	(yes)	(yes)

Thank you for your attention.
Time for your questions.



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